



Statistical Machine Learning

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Course Information

- ▶ Course web:
 - ▶ <https://yao-lab.github.io/course/statml/>
- ▶ Time and Venue:
 - ▶ Lecture: **Mon, 6:30-9:20pm**
 - ▶ Room 4579, Lift 27-28
- ▶ Instructor:
 - ▶ Yuan Yao <yuany@ust.hk> (<https://yao-lab.github.io/>)
- ▶ Teaching Assistant:
 - ▶ ???



Course Content

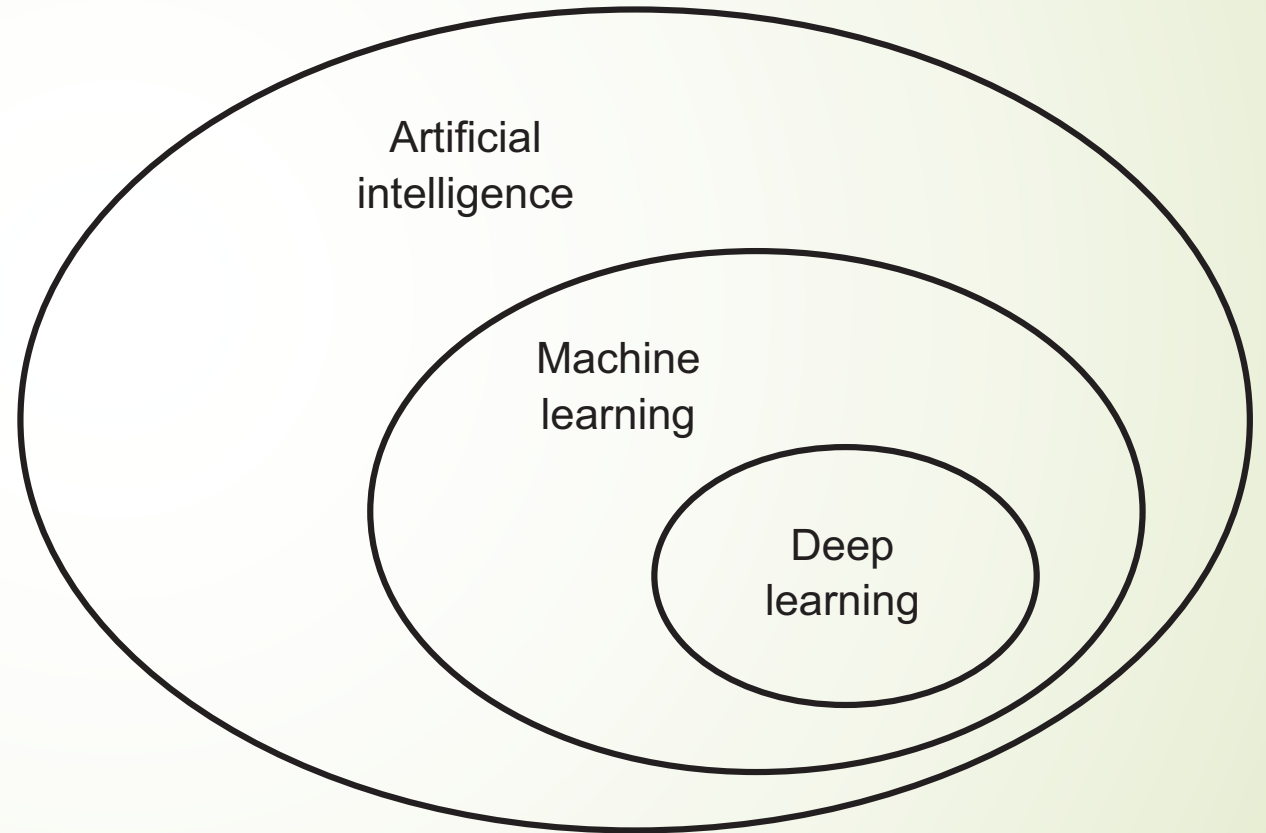
- ▶ Supervised Learning:
 - ▶ working knowledge about linear regression, classification, logistic regression, decision trees (CART), boosting, random forests, support vector machines, neural networks, etc.
- ▶ Unsupervised and Self-supervised Learning:
 - ▶ PCA, Generative Models, Generative Adversarial Networks
 - ▶ Self-supervision, e.g. masked language models etc.
- ▶ Reinforcement Learning:
 - ▶ Markov Decision Process and online learning, etc.
- ▶ **No exams. Project-based evaluation.**



A Brief History of AI, Machine Learning, and Deep Learning

Artificial Intelligence, Machine Learning, and Deep Learning

- ▶ AI is born in 1950s, when a handful of pioneers from the nascent field of computer science started asking **whether computers could be made to “think”**—a question whose ramifications we’re still exploring today.

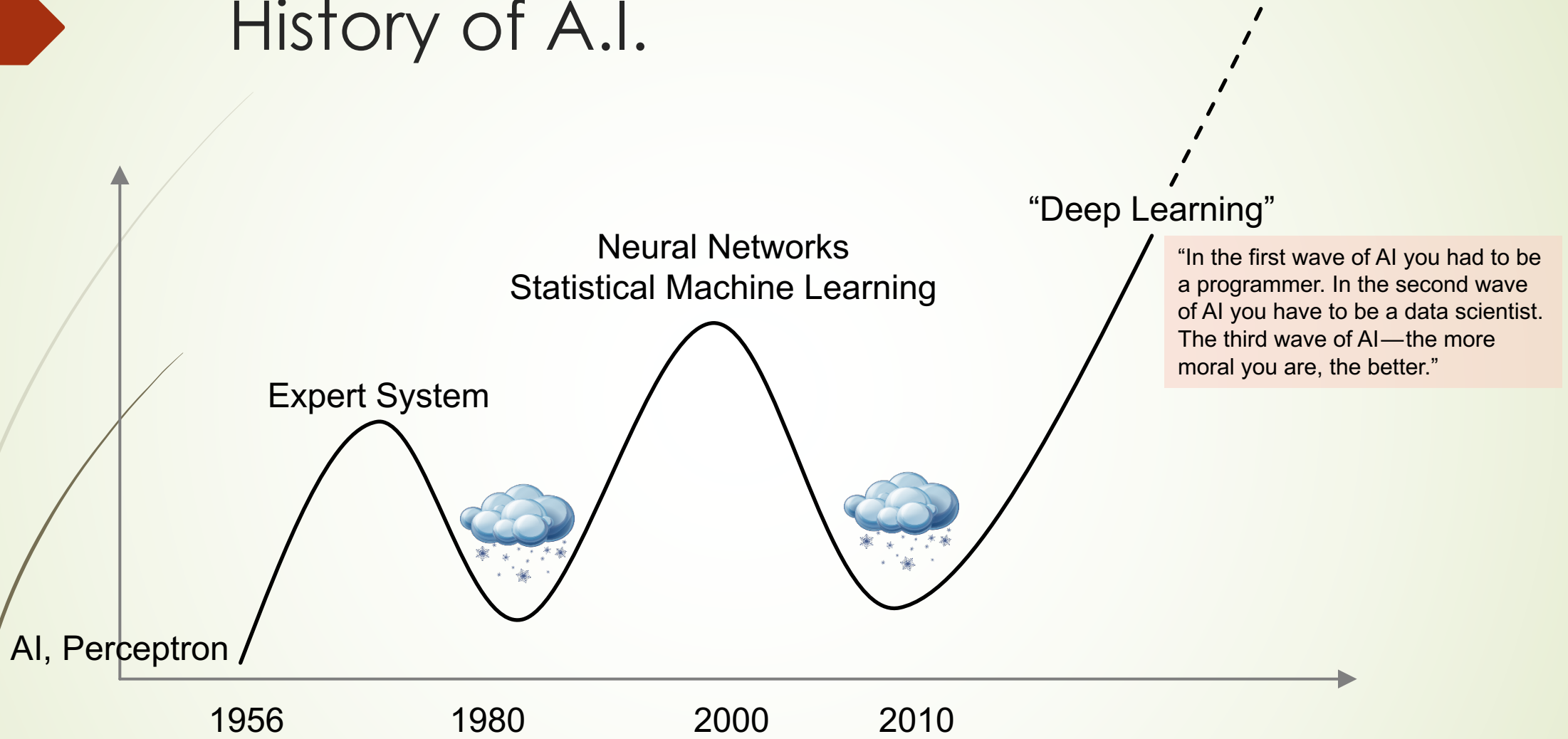


A brief history of AI



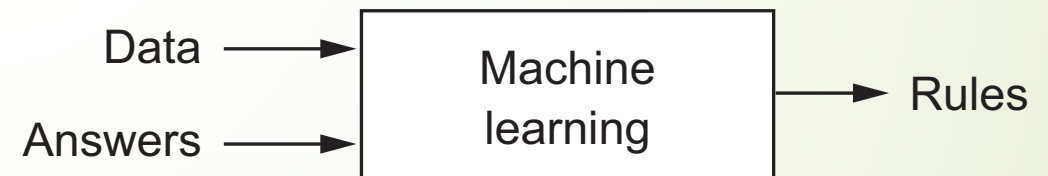
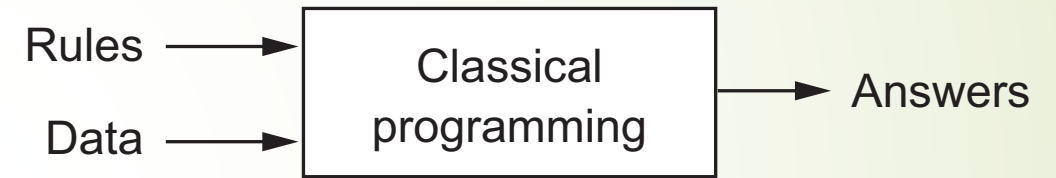
- **1943:** McCulloch & Pits proposed a boolean circuit model of neurons
- **1949:** Donald Hebb proposed **Hebbian learning rule**.
- **1950:** Alan Turing published "**Computing Machinery and Intelligence**" with **Turing test**.
- **1956:** John McCarthy at the Dartmouth Conference coined terminology "**Artificial Intelligence**"
- **1957:** Rosenblatt invented **Perceptron**
- **1960s:** golden years till **1969 Minsky-Papert's** critical book **Perceptron**
- **1970s:** the first AI winter
- **1980s:** boom of AI with **Expert System**
- **1990s:** the second AI winter, rise of **statistical machine learning**
- **1997: IBM Deep Blue** beats world chess champion Kasparov
- **2012:** return of neural networks as **deep learning** (speech, ImageNet in computer vision, NLP, ...)
- **2016-2017: Google AlphaGo "Lee" and Zero**
- **2020: Google AlphaFold**
- ...

History of A.I.



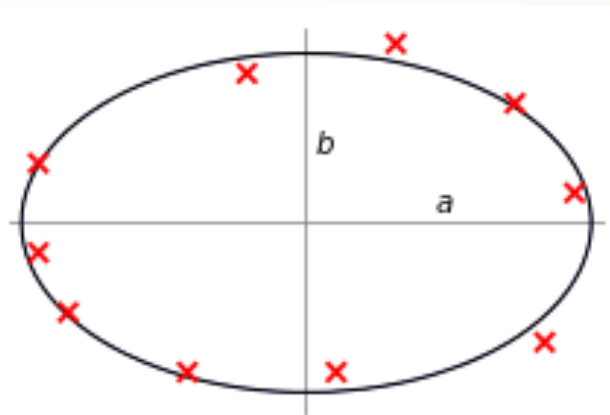
Statistical Machine Learning is a new paradigm of computer programming

- ▶ During 1950s-1980s, two competitive ideas of realizing AI exist
 - ▶ Rule based inference, or called **Expert System**
 - ▶ Statistics based inference, or called **Machine Learning**
- ▶ 1990s- Machine Learning becomes dominant



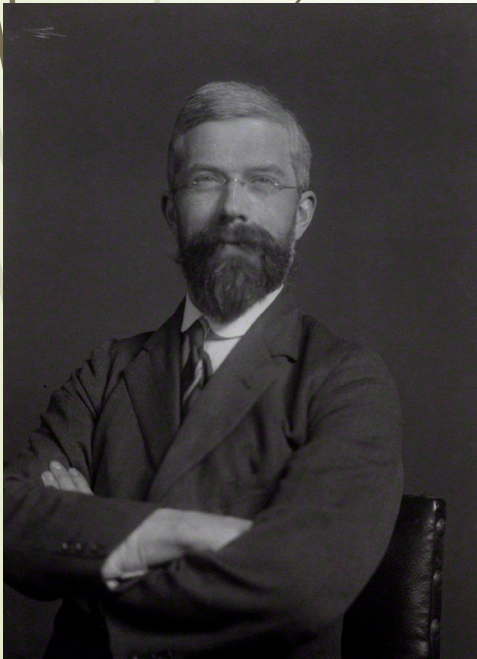
The 1st machine learning method: Least Squares

- Invention:
 - **Carl Friedrich Gauss** (~1795/1809/1810),
 - Adrien-Marie Legendre (1805)
 - Robert Adrain (1808)
- Application:
 - Prediction of the location of asteroid Ceres after it emerged from behind the sun (Franz Xaver von Zach 1801)
 - Orbits of planets, Newton Laws
 - Statistics,
 - ...



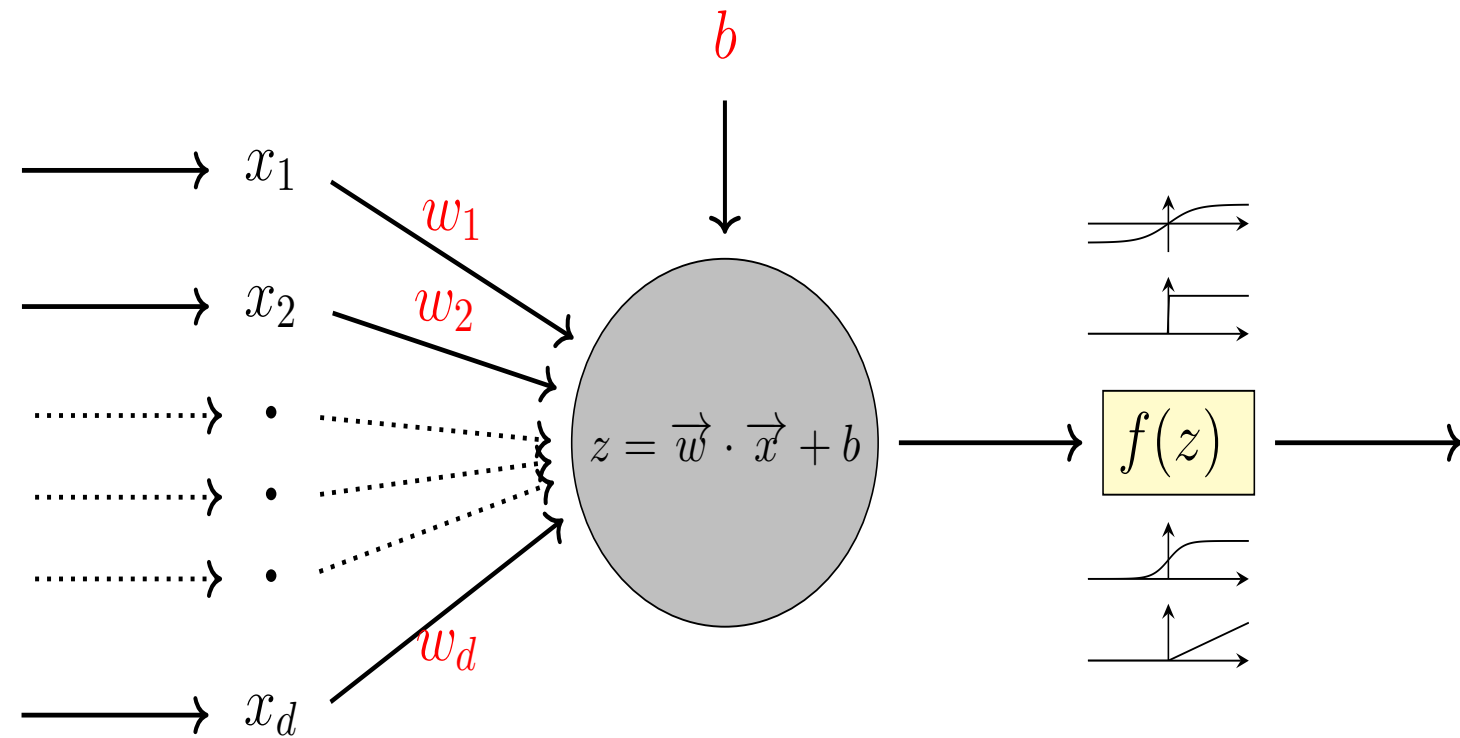
Fisher's Maximum Likelihood Principle (1912-1922)

- **The least square method is the maximum likelihood estimate** (most probable values of the unknown parameters) when the noise is Gaussian.
- Fisher, R. A. (1912) **On an absolute criterion for fitting frequency curves.** *Messenger of Mathematics* 41:155-160.
- Fisher, R. A. (1922). **On the mathematical foundations of theoretical statistics.** *Philos. Trans. Roy. Soc. London Ser. A* 222:309-368.
- Aldrich, John (1997). **R. A. Fisher and the Making of Maximum Likelihood 1912 -- 1922.** *Statistical Science*, 12(3):162-176.



The 1st neural network: Perceptron

- Invented by Frank Rosenblatt (1957)



The Perceptron Algorithm for classification

$$\ell(w) = - \sum_{i \in \mathcal{M}_w} y_i \langle w, \mathbf{x}_i \rangle, \quad \mathcal{M}_w = \{i : y_i \langle \mathbf{x}_i, w \rangle < 0, y_i \in \{-1, 1\}\}.$$

The Perceptron Algorithm is a *Stochastic Gradient Descent* method (**Robbins-Monro 1951**, *Ann. Math. Statist.* 22(3): 400-407):

$$\begin{aligned} w_{t+1} &= w_t - \eta_t \nabla_i \ell(w) \\ &= \begin{cases} w_t - \eta_t y_i \mathbf{x}_i, & \text{if } y_i w_t^T \mathbf{x}_i < 0, \\ w_t, & \text{otherwise.} \end{cases} \end{aligned}$$

Finiteness of Stopping Time and Margin

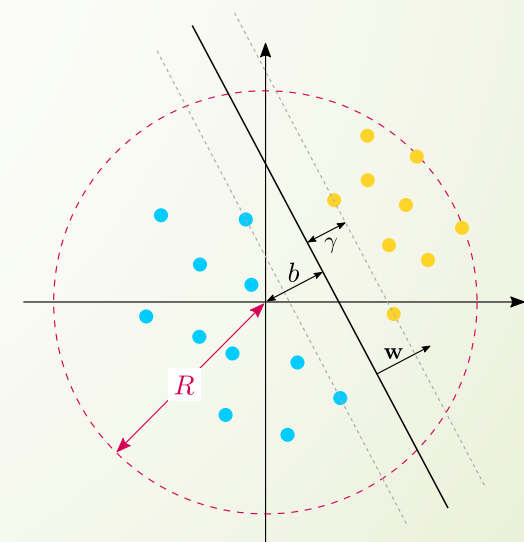
The perceptron convergence theorem was proved by Block (1962) and Novikoff (1962). The following version is based on that in Cristianini and Shawe-Taylor (2000).

Theorem 1 (Block, Novikoff). *Let the training set $S = \{(\mathbf{x}_1, t_1), \dots, (\mathbf{x}_n, t_n)\}$ be contained in a sphere of radius R about the origin. Assume the dataset to be linearly separable, and let \mathbf{w}_{opt} , $\|\mathbf{w}_{\text{opt}}\| = 1$, define the hyperplane separating the samples, having functional margin $\gamma > 0$. We initialise the normal vector as $\mathbf{w}_0 = \mathbf{0}$. The number of updates, k , of the perceptron algorithms is then bounded by*

$$k \leq \left(\frac{2R}{\gamma}\right)^2. \quad (10)$$

Input ball: $R = \max_i \|\mathbf{x}_i\|.$

Margin: $\gamma := \min_i y_i f(x_i)$



Hilbert's 13th Problem

Algebraic equations (under a suitable transformation) of degree up to 6 can be solved by functions of two variables. What about

$$x^7 + ax^3 + bx^2 + cx + 1 = 0?$$

Hilbert's conjecture: $x(a, b, c)$ cannot be expressed by a superposition (sums and compositions) of bivariate functions.

Question: can every continuous (analytic, C^∞ , etc) function of n variables be represented as a superposition of continuous (analytic, C^∞ , etc) functions of $n - 1$ variables?

Theorem (D. Hilbert)

There is an analytic function of three variables that cannot be expressed as a superposition of bivariate ones.



Kolmogorov's Superposition Theorem

Theorem (A. Kolmogorov, 1956; V. Arnold, 1957)

Given $n \in \mathbb{Z}^+$, every $f_0 \in C([0, 1]^n)$ can be represented as

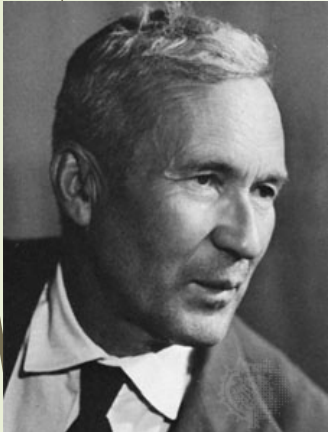
$$f_0(x_1, x_2, \dots, x_n) = \sum_{q=1}^{2n+1} g_q \left(\sum_{p=1}^n \phi_{pq}(x_p) \right),$$

where $\phi_{pq} \in C[0, 1]$ are increasing functions independent of f_0 and $g_q \in C[0, 1]$ depend on f_0 .

- Can choose g_q to be all the same $g_q \equiv g$ (Lorentz, 1966).
- Can choose ϕ_{pq} to be Hölder or Lipschitz continuous, but not C^1 (Fridman, 1967).
- Can choose $\phi_{pq} = \lambda_p \phi_q$ where $\lambda_1, \dots, \lambda_n > 0$ and $\sum_p \lambda_p = 1$ (Sprecher, 1972).

If f is a multivariate continuous function, then f can be written as a superposition of composite functions of mixtures of continuous functions of single variables:

finite **composition** of continuous functions of a **single variable** and the **addition**.



Kolmogorov's Exact Representation is not stable or smooth

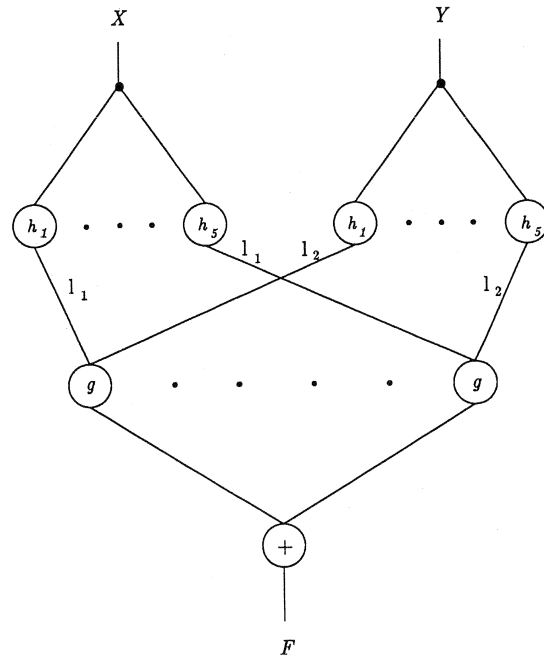


Figure 1: The network representation of an improved version of Kolmogorov's theorem, due to Kahane (1975). The figure shows the case of a bivariate function. The Kahane's representation formula is $f(x_1, \dots, x_n) = \sum_{q=1}^{2n+1} g[\sum_{p=1}^n l_p h_q(x_p)]$ where h_q are strictly monotonic functions and l_p are strictly positive constants smaller than 1.



- [Girosi-Poggio' 1989] Representation Properties of Networks: Kolmogorov's Theorem Is Irrelevant, <https://www.mitpressjournals.org/doi/pdf/10.1162/neco.1989.1.4.465>
- Lacking smoothness in h and g [Vitushkin' 1964] fails to guarantee the **generalization ability (stability)** against noise and perturbations
- The representation is **not universal** in the sense that g and h both depend on the function F to be represented.

Universal Approximate Representation

[Cybenko' 1989, Hornik et al. 1989, Poggio-Girosi' 1989, ...]

For continuous $f : [0, 1]^N \rightarrow \mathbb{R}$ and $\varepsilon > 0$ there exists

$$\begin{aligned} F(x) &= \alpha^\top \sigma(Wx + \beta) \\ &= \sum_i \alpha_i \sigma \left(\sum_j W_{i,j} x_j + \beta_i \right) \end{aligned}$$

such that for all x in $[0, 1]^N$ we have $|F(x) - f(x)| < \varepsilon$.

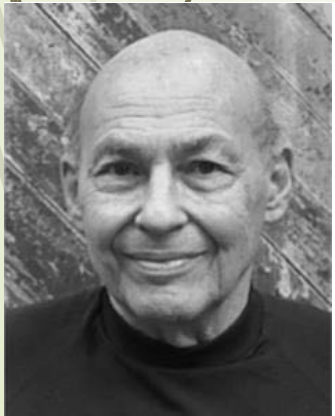
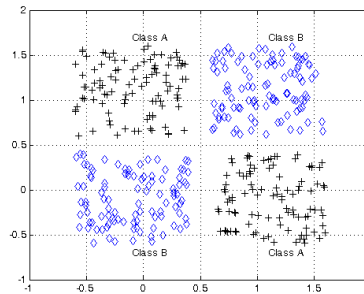
Complexity (regularity, smoothness) thereafter becomes the central pursuit in Approximation Theory.

Locality or Sparsity of Computation

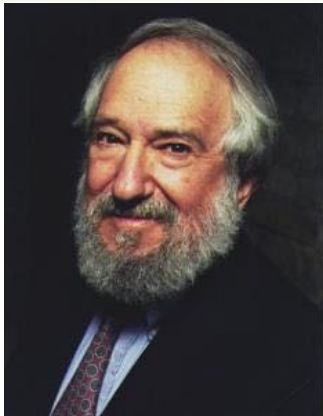
Minsky and Papert, 1969

Perceptron can't do **XOR** classification

Perceptron needs infinite global information to compute **connectivity**



Marvin Minsky

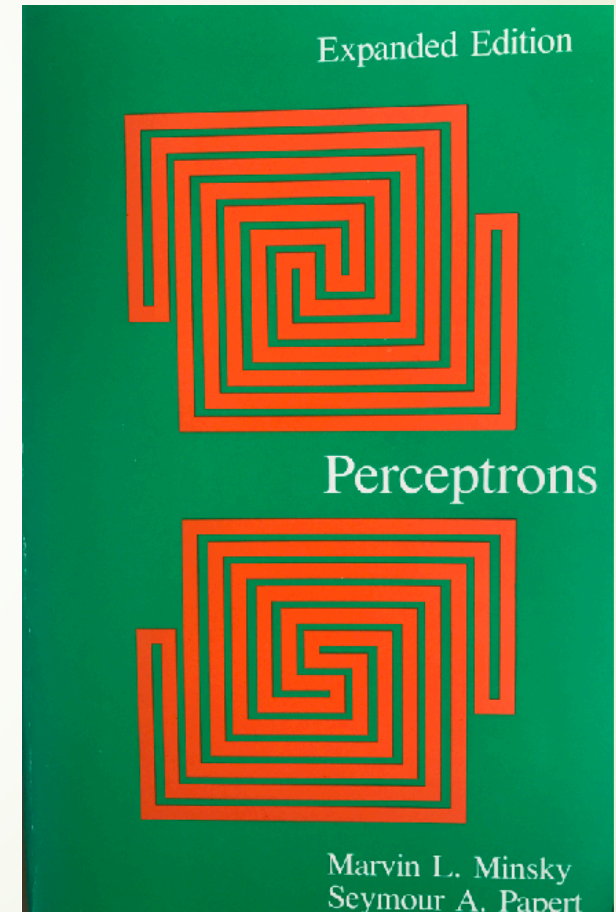


Seymour Papert

Locality or **Sparsity** is important:

Locality in time?

Locality in space?



Multilayer Perceptrons (MLP) and Back-Propagation (BP) Algorithms

D.E. Rumelhart, G. Hinton, R.J. Williams (1986)

Learning representations by back-propagating errors, *Nature*, 323(9): 533-536

BP algorithms as **stochastic gradient descent** algorithms (**Robbins–Monro 1950; Kiefer-Wolfowitz 1951**) with Chain rules of Gradient maps

Deep network may classify **XOR**. Yet **topology**?

We address complexity and geometric invariant properties first.



NATURE VOL. 323 9 OCTOBER 1986 LETTERS TO NATURE 533

Learning representations by back-propagating errors

David E. Rumelhart*, Geoffrey E. Hinton† & Ronald J. Williams*

* Institute for Cognitive Science, C-015, University of California, San Diego, La Jolla, California 92093, USA
 † Department of Computer Science, Carnegie-Mellon University, Pittsburgh, Philadelphia 15213, USA

We describe a new learning procedure, back-propagation, for networks of neuron-like units. The procedure repeatedly adjusts the weights of the connections in the network so as to minimize a measure of the difference between the actual output vector of the net and the desired output vector. As a result of the weight adjustments, internal 'hidden' units which are not part of the input or output come to represent important features of the task domain, and the regularities in the task are captured by the interactions of these units. The ability to create useful new features distinguishes back-propagation from earlier, simpler methods such as the perceptron-convergence procedure¹.

There have been many attempts to design self-organizing neural networks. The aim is to find a powerful synaptic modification rule that will allow an arbitrarily connected neural network to develop an internal structure that is appropriate for a particular task domain. The task is specified by giving the desired state vector of the output units for each state vector of the input units. If the input units are directly connected to the output units it is relatively easy to find learning rules that iteratively adjust the relative strengths of the connections so as to progressively reduce the difference between the actual and desired output vectors². Learning becomes more interesting but more difficult when we introduce hidden units whose actual or desired states are not specified by the task. (In perceptrons, there are 'feature analysers' between the input and output that are not true hidden units because their input connections are fixed by hand, so their states are completely determined by the input vector; they do not learn representations.) The learning procedure must decide under what circumstances the hidden units should be active in order to help achieve the desired input-output behaviour. This amounts to deciding what these units should represent. We demonstrate that a general purpose and relatively simple procedure is powerful enough to construct appropriate internal representations.

The simplest form of the learning procedure is for layered networks which have a layer of input units at the bottom; any number of intermediate layers; and a layer of output units at the top. Connections within a layer or from higher to lower layers are forbidden, but connections can skip intermediate layers. An input vector is presented to the network by setting the states of the input units. Then the states of the units in each layer are determined by applying equations (1) and (2) to the connections coming from lower layers. All units within a layer have their states set in parallel, but different layers have their states set sequentially, starting at the bottom and working upwards until the states of the output units are determined.

The total input, x_j , to unit j is a linear function of the outputs, y_i , of the units that are connected to j and of the weights, w_{ji} , on these connections

$$x_j = \sum_i y_i w_{ji} \quad (1)$$

Units can be given biases by introducing an extra input to each unit which always has a value of 1. The weight on this extra input is called the bias and is equivalent to a threshold of the opposite sign. It can be treated just like the other weights.

A unit has a real-valued output, y_j , which is a non-linear function of its total input

$$y_j = \frac{1}{1 + e^{-x_j}} \quad (2)$$

¹ To whom correspondence should be addressed

Parallel Distributed Processing

by Rumelhart and McClelland, 1986

Minsky and Papert set out to show which functions can and cannot be computed by this class of machines. They demonstrated, in particular, that such perceptrons are unable to calculate such mathematical functions as parity (whether an odd or even number of points are on in the retina) or the topological function of connectedness (whether all points that are on are connected to all other points that are on either directly or via other points that are also on) without making use of absurdly large numbers of predicates. The analysis is extremely elegant and demonstrates the importance of a mathematical approach to analyz-

of multilayer networks that compute parity). Similarly, it is not difficult to develop networks capable of solving the connectedness or inside/outside problem. Hinton and Sejnowski have analyzed a version of such a network (see Chapter 7).

Essentially, then, although Minsky and Papert were exactly correct in their analysis of the *one-layer perceptron*, the theorems don't apply to systems which are even a little more complex. In particular, it doesn't apply to multilayer systems nor to systems that allow feedback loops.





Topology can be learned with finite
information if the manifold is *stable*

Blum-Shub-Smale models of Real Computation

A Model of Real Computation

- ▶ Starting from **Blum, Shub, Smale** (1989)
- ▶ It admits inputs and operations (addition, subtraction, multiplication, and (in the case of fields) division) of **real (complex) numbers** with *infinite precision*
- ▶ “The key importance of the **condition number**, which measures the closeness of a problem instance to the manifold of ill-posed instances, is clearly developed.” – [Richard Karp](#)



The Condition Number of a Manifold

Throughout our discussion, we associate to \mathcal{M} a condition number $(1/\tau)$ where τ is defined as the largest number having the property: The open normal bundle about \mathcal{M} of radius r is embedded in \mathbb{R}^N for every $r < \tau$. Its image Tub_τ is a tubular neighborhood of \mathcal{M} with its canonical projection map

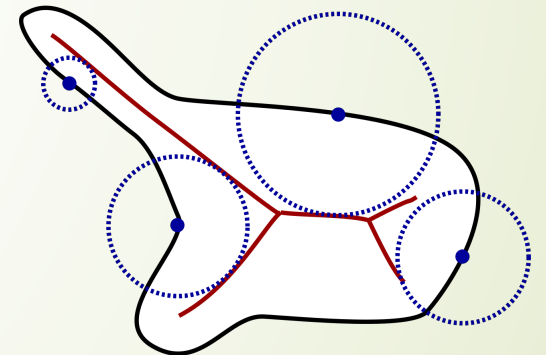
$$\pi_0 : \text{Tub}_\tau \rightarrow \mathcal{M}.$$

Smallest Local Feature Size

$$G = \{x \in \mathbb{R}^N \text{ such that } \exists \text{ distinct } p, q \in \mathcal{M} \text{ where } d(x, \mathcal{M}) = \|x - p\| = \|x - q\|\},$$

where $d(x, \mathcal{M}) = \inf_{y \in \mathcal{M}} \|x - y\|$ is the distance of x to \mathcal{M} . The closure of G is called the medial axis and for any point $p \in \mathcal{M}$ the local feature size $\sigma(p)$ is the distance of p to the medial axis. Then it is easy to check that

$$\tau = \inf_{p \in \mathcal{M}} \sigma(p).$$



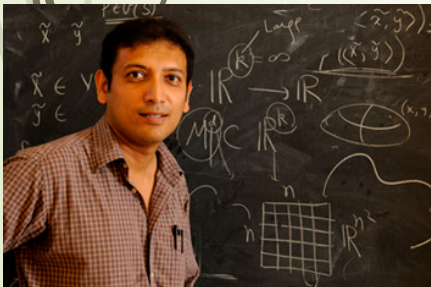
Find Homology with Finite Samples

[Niyogi, Smale, Weinberger (2008)]

Theorem 3.1 *Let \mathcal{M} be a compact submanifold of \mathbb{R}^N with condition number τ . Let $\bar{x} = \{x_1, \dots, x_n\}$ be a set of n points drawn in i.i.d. fashion according to the uniform probability measure on \mathcal{M} . Let $0 < \epsilon < \tau/2$. Let $U = \bigcup_{x \in \bar{x}} B_\epsilon(x)$ be a correspondingly random open subset of \mathbb{R}^N . Then for all*

$$n > \beta_1 \left(\log(\beta_2) + \log\left(\frac{1}{\delta}\right) \right),$$

the homology of U equals the homology of \mathcal{M} with high confidence (probability $> 1 - \delta$).



Partha Niyogi@Chicicago,
1967-2010

$$\beta_1 = \frac{\text{vol}(\mathcal{M})}{(\cos^k(\theta_1))\text{vol}(B_{\epsilon/4}^k)} \quad \text{and} \quad \beta_2 = \frac{\text{vol}(\mathcal{M})}{(\cos^k(\theta_2))\text{vol}(B_{\epsilon/8}^k)}.$$

Here k is the dimension of the manifold \mathcal{M} and $\text{vol}(B_\epsilon^k)$ denotes the k -dimensional volume of the standard k -dimensional ball of radius ϵ . Finally, $\theta_1 = \arcsin(\epsilon/8\tau)$ and $\theta_2 = \arcsin(\epsilon/16\tau)$.

Convolutional Neural Networks: shift invariances and locality

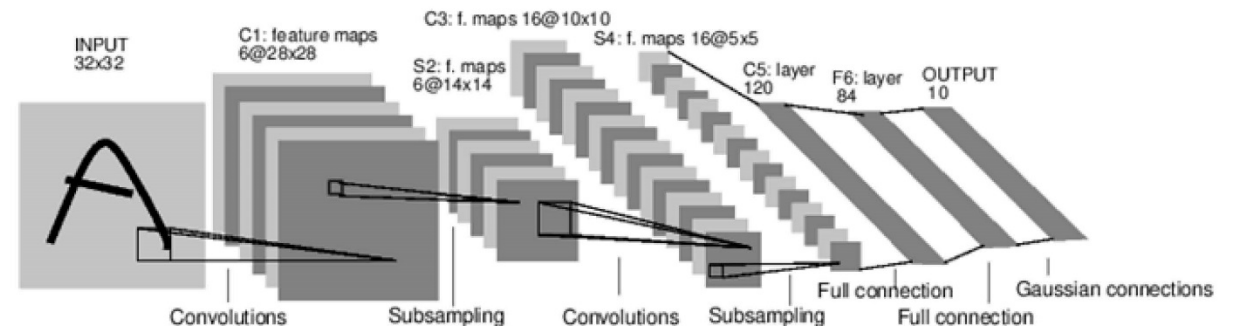
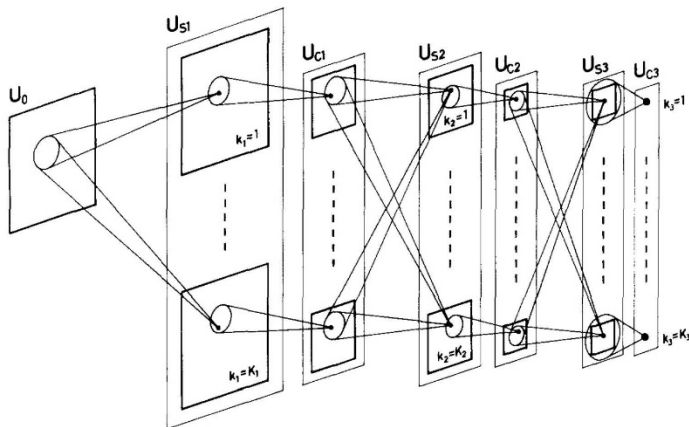
- Can be traced to *Neocognitron* of Kunihiko Fukushima (1979)
- Yann LeCun combined convolutional neural networks with back propagation (1989)
- Imposes **shift invariance** and **locality** on the weights
- Forward pass remains similar
- Backpropagation slightly changes – need to sum over the gradients from all spatial positions

Biol. Cybernetics 36, 193–202 (1980)

Neocognitron: A Self-organizing Neural Network Model for a Mechanism of Pattern Recognition Unaffected by Shift in Position

Kunihiko Fukushima

NHK Broadcasting Science Research Laboratories, Kinuta, Setagaya, Tokyo, Japan

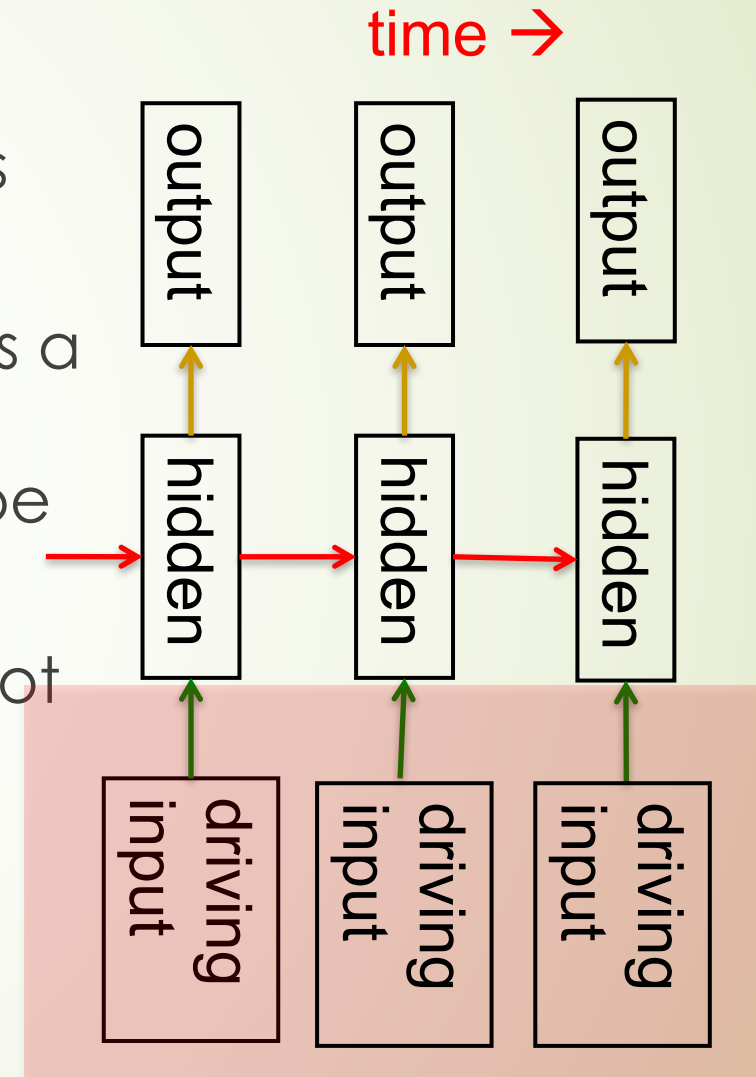


Time series: Linear Dynamical Systems (1940s-)

- ▶ The hidden state has linear dynamics with Gaussian noise and produces the observations using a linear model with Gaussian noise.
- ▶ Kalman Filter: A linearly transformed Gaussian is a Gaussian. So the distribution over the hidden state given the data so far is Gaussian. It can be computed using “Kalman filtering”.
- ▶ To predict the next output (so that we can shoot down the missile) we need to infer the hidden state.

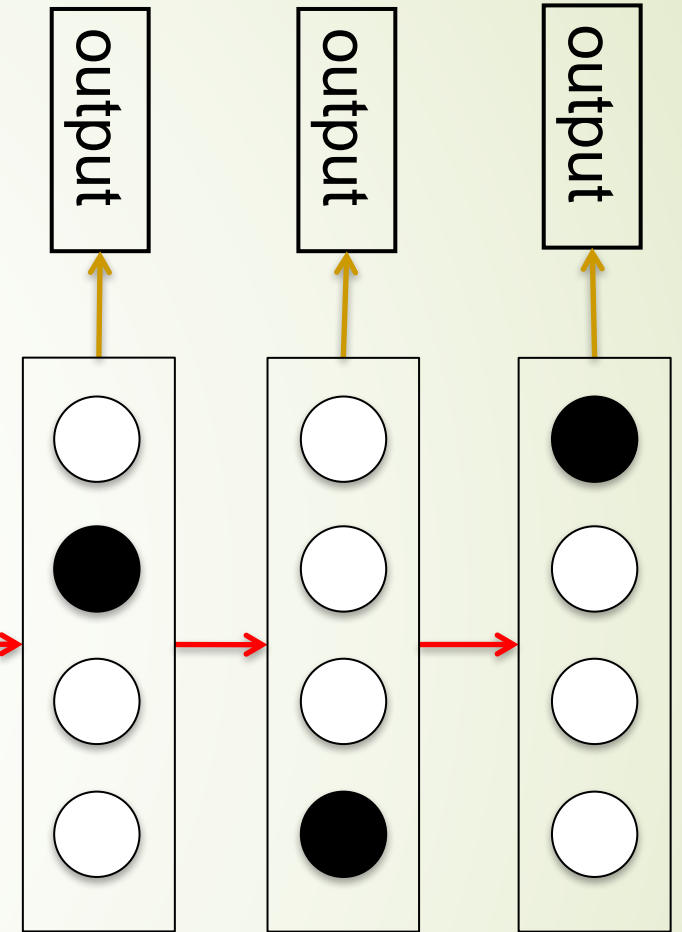
$$h_t = W_{hh}h_{t-1} + W_{hx}x_t + \epsilon_t^h$$

$$y_t = W_{yh}h_t + W_{yx}x_t + \epsilon_t^y$$

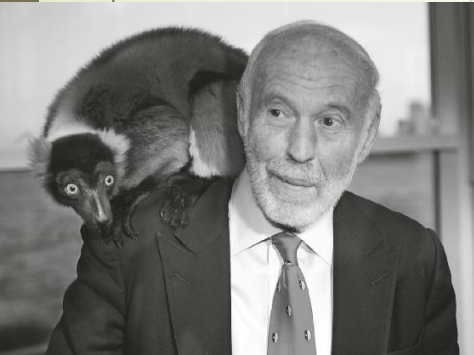


Hidden Markov Models (1970s-)

- Hidden Markov Models have a discrete one-of-N hidden state. Transitions between states are stochastic and controlled by a transition matrix. The outputs produced by a state are stochastic.
- We cannot be sure which state produced a given output. So the state is “hidden”.
- It is easy to represent a probability distribution across N states with N numbers.
- To predict the next output we need to infer the probability distribution over hidden states.
 - HMMs have efficient algorithms (**Baum-Welch or EM Algorithm**) for inference and learning.
 - **Jim Simons** hires Lenny Baum as the founding member of Renaissance Technologies in 1979



time →



Lenny Baum became a devoted Go player despite his deteriorating eyesight.

Recurrent Neural Networks (1986-)

- **The issue of a hidden Markov model (HMM):**

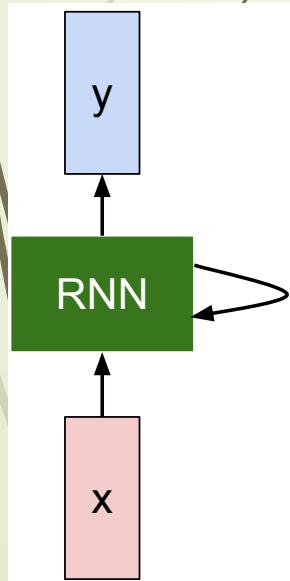
- At each time step it must select one of its hidden states. So with N hidden states it can only remember $\log(N)$ bits about what it generated so far.

- RNNs are very powerful, because they combine two properties:

- Distributed hidden state that allows them to store a lot of information about the past efficiently.
- Non-linear dynamics that allows them to update their hidden state in complicated ways.

- Rumelhart et al. enables training by **BP** algorithm

- With enough neurons and time, RNNs can compute anything that can be computed by your computer.

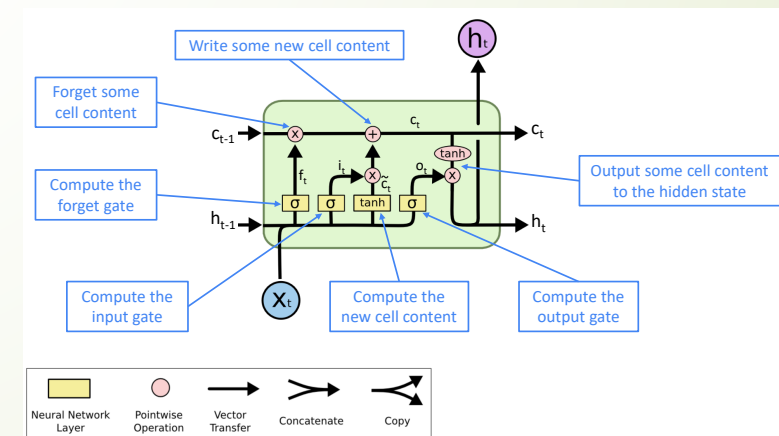


$$h_t = \sigma_h(W_{hh}h_{t-1} + W_{hx}x_t)$$

$$y_t = \sigma_y(W_{yh}h_t)$$

Long-Short-Term-Memory (LSTM)

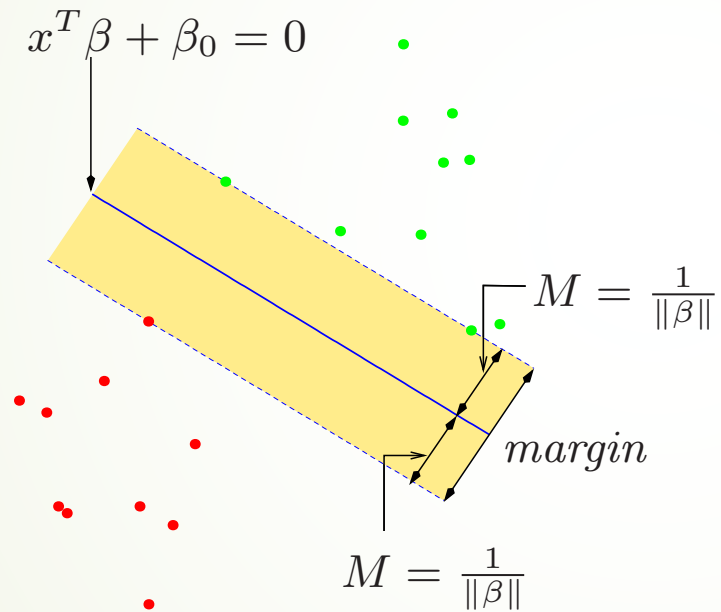
- [Sepp Hochreiter; Jürgen Schmidhuber \(1997\). "Long short-term memory". *Neural Computation*. 9 \(8\): 1735–1780. \(https://www.bioinf.jku.at/publications/older/2604.pdf\)](https://www.bioinf.jku.at/publications/older/2604.pdf)
- Introduction of short path to learn deep networks without vanishing gradient problem.



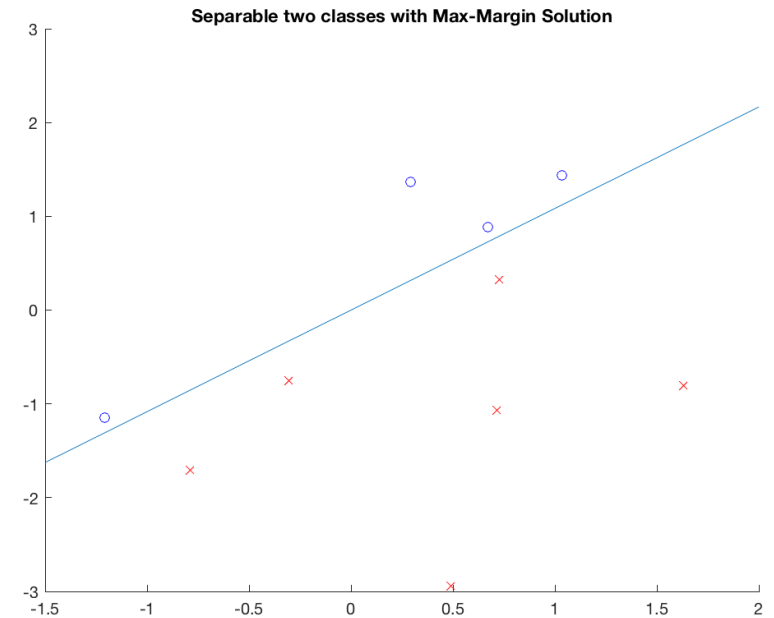
Max-Margin Classifier (SVM)

$$\text{minimize}_{\beta_0, \beta_1, \dots, \beta_p} \|\beta\|^2 := \sum_j \beta_j^2$$

subject to $y_i(\beta_0 + \beta_1 x_{i1} + \dots + \beta_p x_{ip}) \geq 1$ for all i



Vladimir Vapnik, 1994



MNIST Dataset Test Error

LeCun et al. 1998



Simple SVM performs
as well as Multilayer
Convolutional Neural
Networks which need
careful tuning (LeNets)

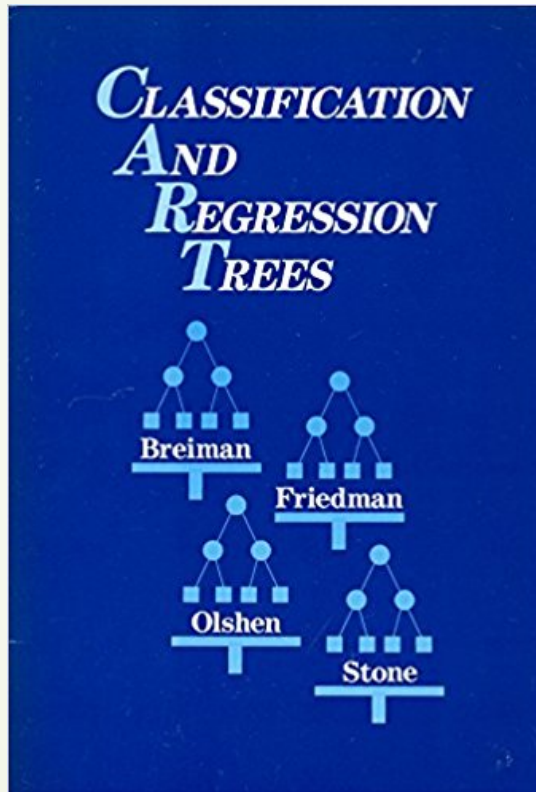
Dark era for NN: 1998-2012



2000-2010: The Era of SVM, Boosting, ... as nights of Neural Networks



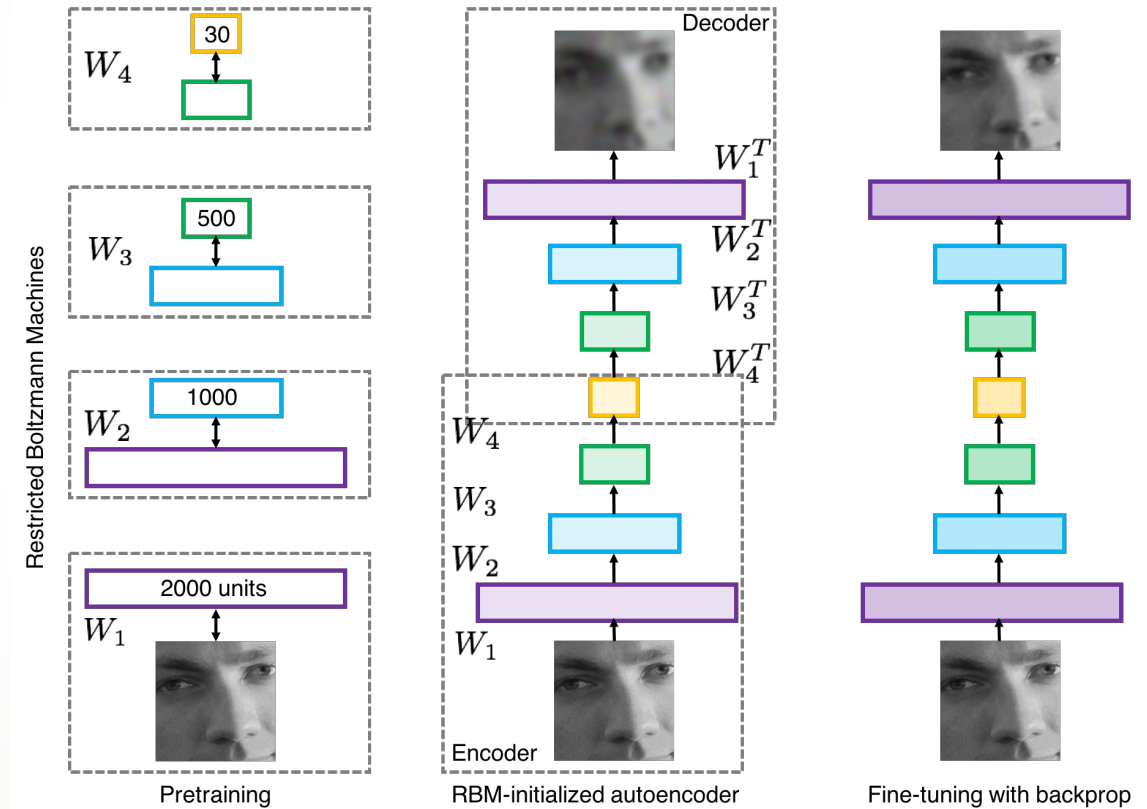
Decision Trees and Boosting



- Breiman, Friedman, Olshen, Stone, (1983): CART
- “The Boosting problem” (M. Kearns & L. Valiant): **Can a set of weak learners create a single strong learner?** (三个臭皮匠顶个诸葛亮?)
- Breiman (1996): Bagging
- Freund, Schapire (1997): **AdaBoost** (“the best off-the-shelf algorithm” by Breiman)
- Breiman (2001): **Random Forests**

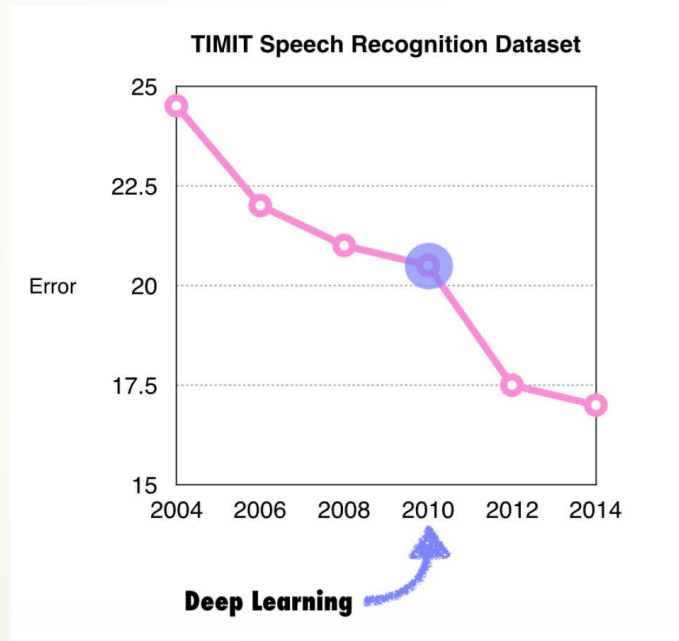
Restricted Boltzman Machine (Deep Learning)

- **Hinton and Salakhutdinov**, Reducing the Dimensionality of Data with Neural Networks, **Science, 2006**
- Reinvigorating research in Deep Learning
- Shows importance of **pretraining (greedy layer-wise, a.k.a. block coordinate descent)**

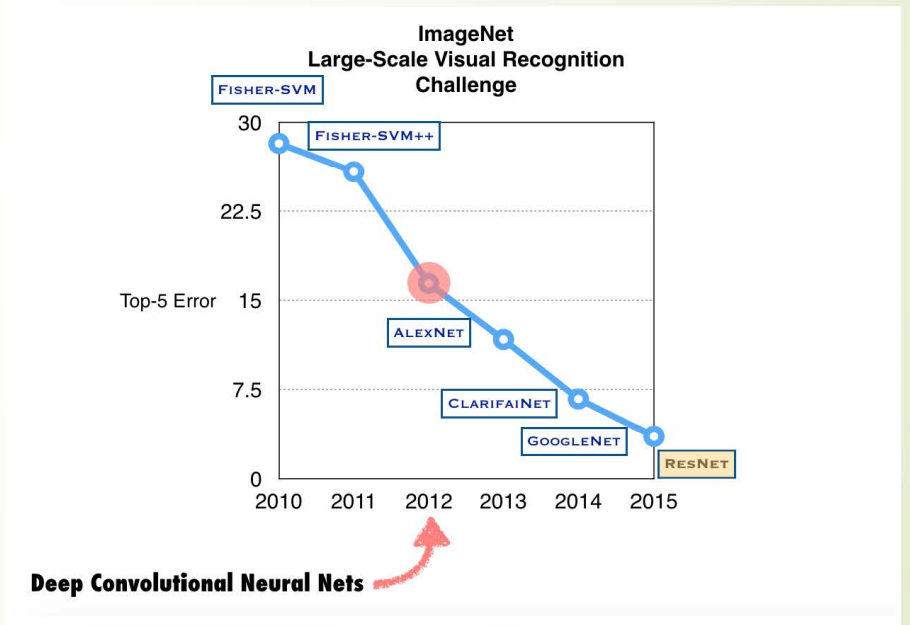


Around the year of 2012: return of NN as 'deep learning'

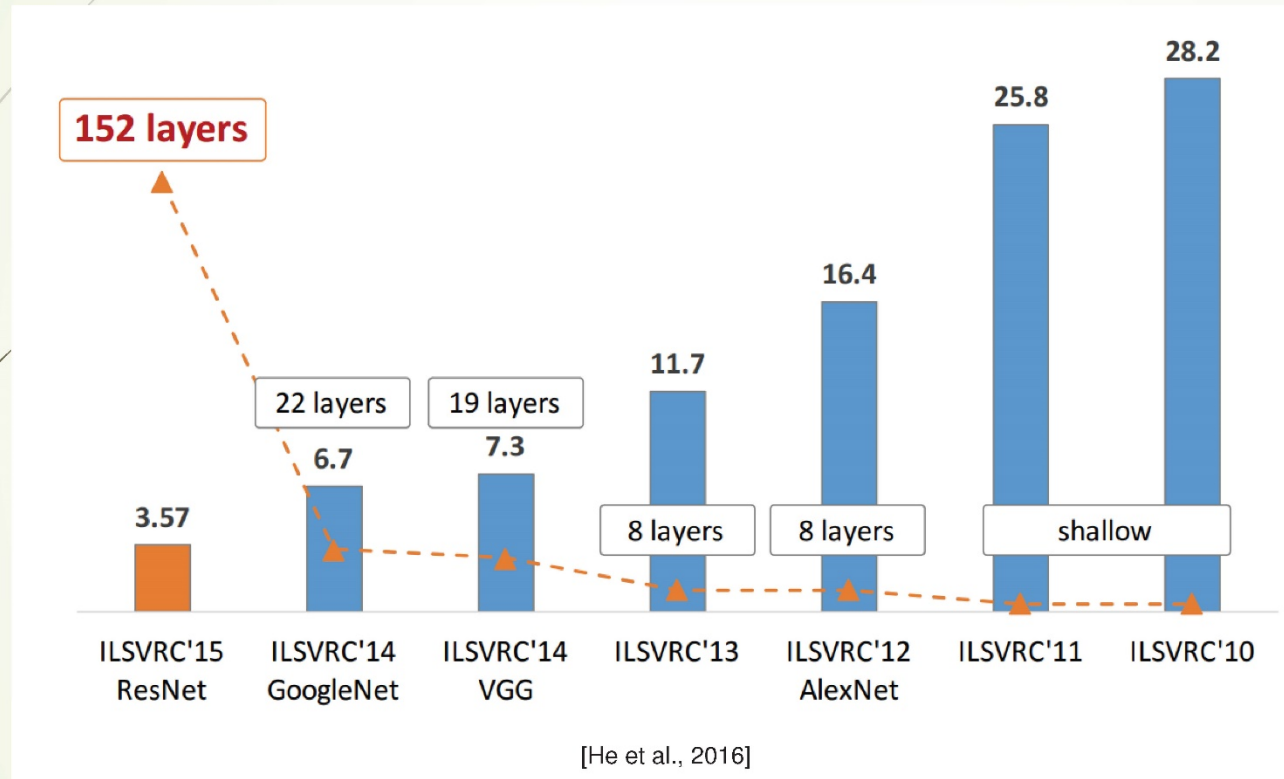
Speech Recognition: TIMIT



Computer Vision: ImageNet

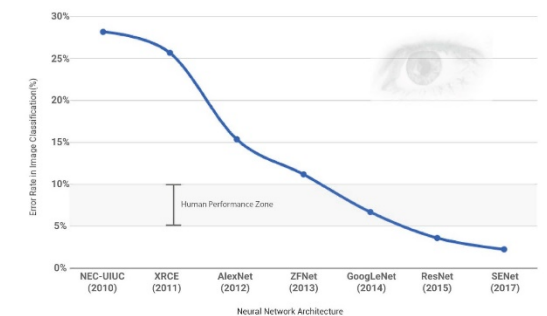


Depth as function of year



ILSVRC ImageNet Top 5 errors

- ImageNet (subset):
 - 1.2 million training images
 - 100,000 test images
 - 1000 classes
- ImageNet large-scale visual recognition Challenge

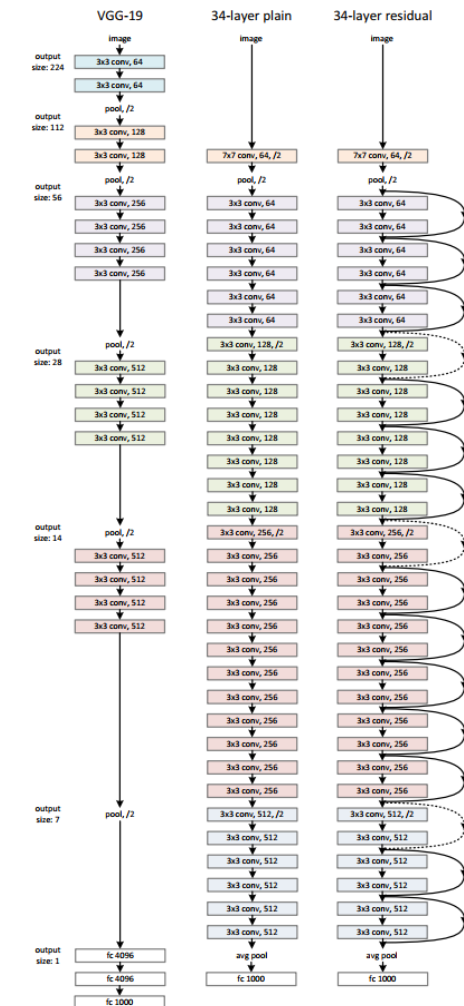
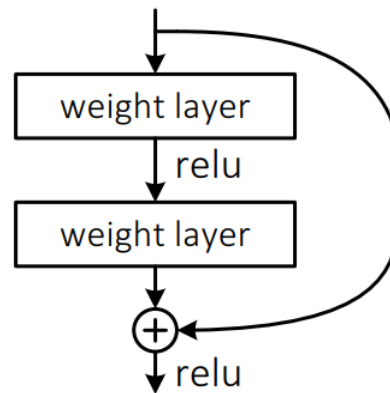


ResNet (2015)

[He-Zhang-Ren-Sun, 2015]

ILSVRC'15 classification winner
(3.57% top 5 error)

- Solves problem by adding skip connections
- Very deep: 152 layers
- No dropout
- Stride
- Batch normalization



Source: Deep Residual Learning for Image Recognition

GPU + Big labeled data

"We're at the beginning of a new day...
This is the beginning of the AI revolution."
— Jensen Huang, GTC Taiwan 2017



兩股力量驅動電腦的未來

深度學習點亮人工智慧紀元。

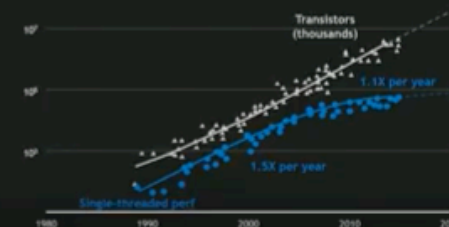
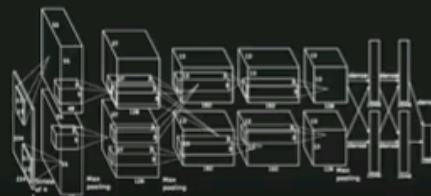
受到人腦的啟發，深度神經網路具備上億的類神經連結，藉由巨量資料來學習，這仰賴極大量的運算。

同時，摩爾定律已到了尾聲 - CPU已不可能再擴張成長。

程式設計人員無法創造出可以更有效率發現更多指令級並行性的CPU架構。

電晶體持續每年增長50%，但是CPU效能僅能成長10%。

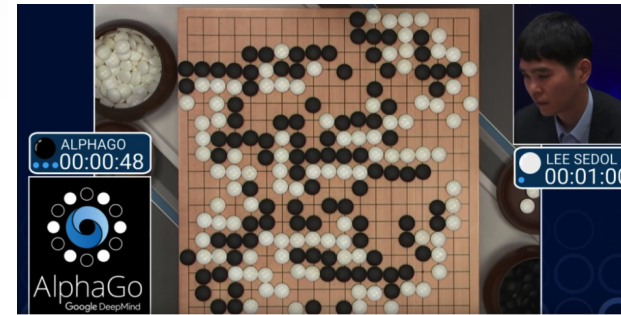
TWO FORCES DRIVING THE FUTURE OF COMPUTING



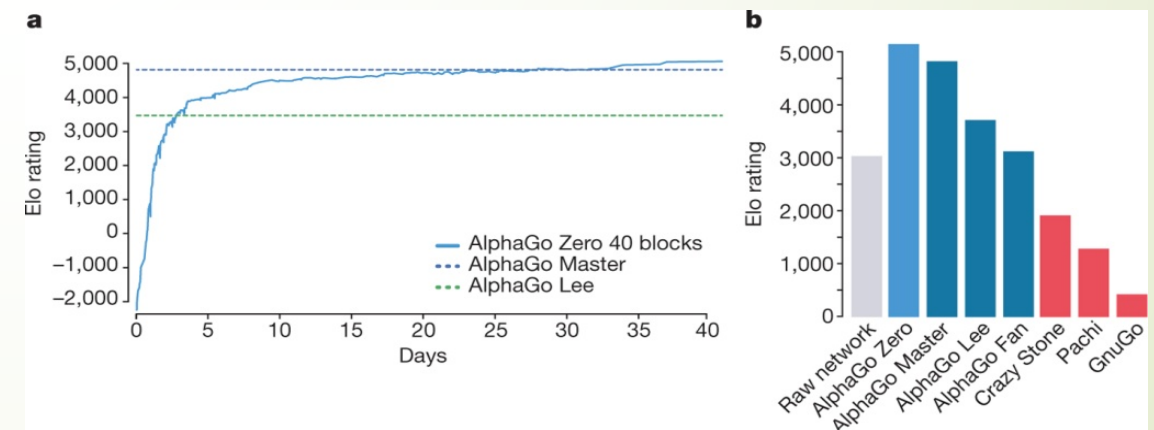
Reaching Human Performance Level in Games



Deep Blue in 1997



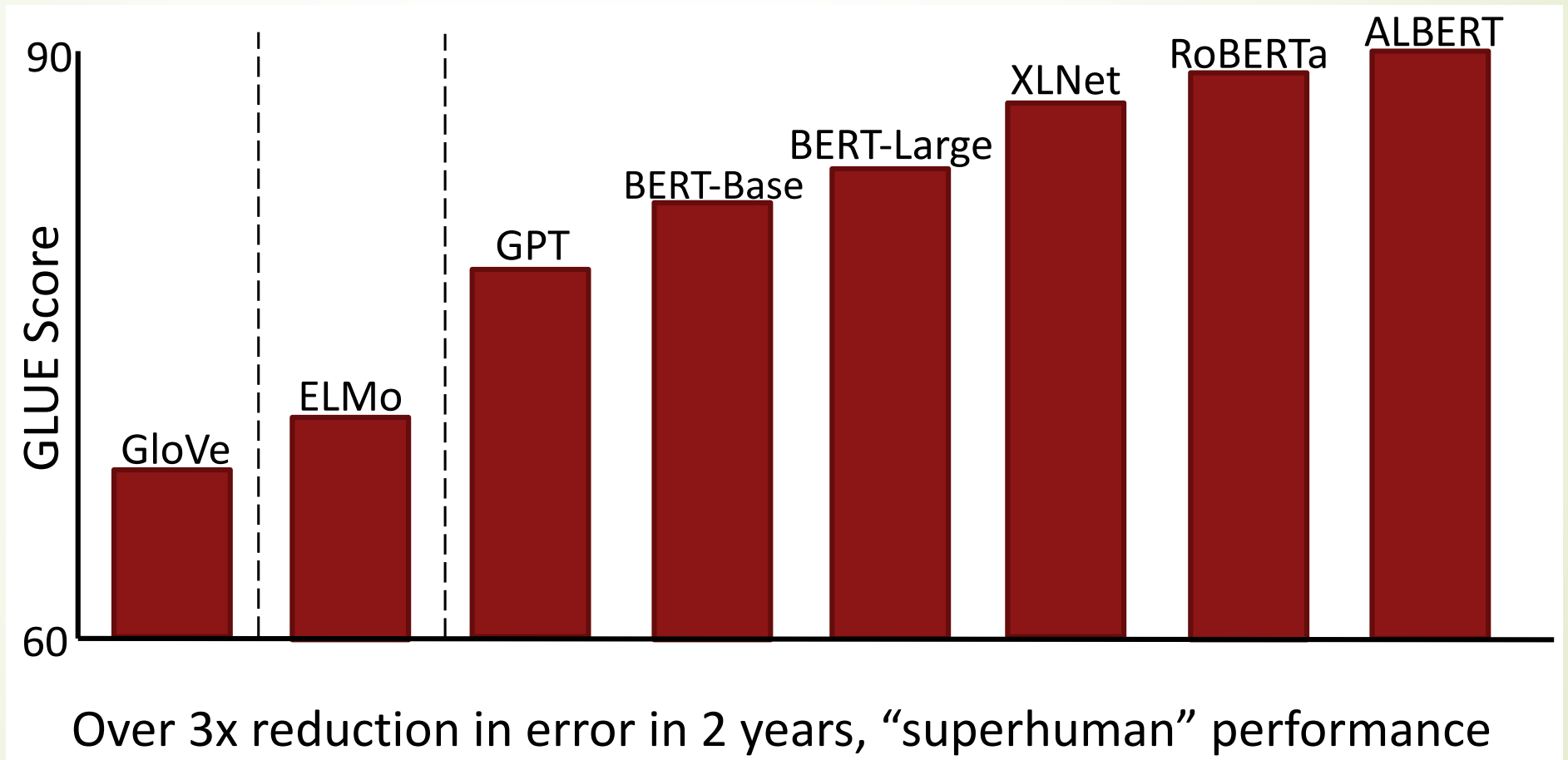
AlphaGo "LEE" 2016



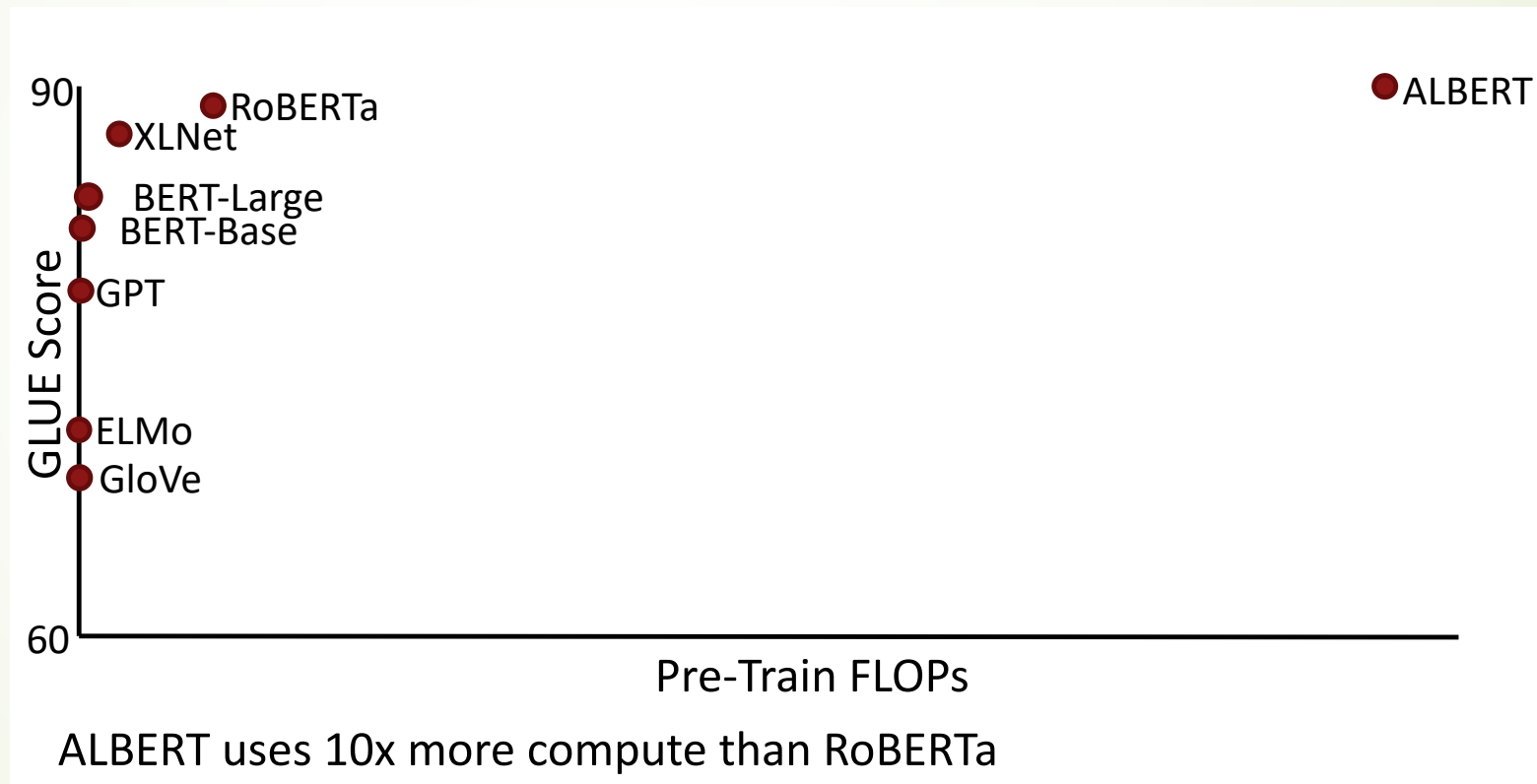
Natural Language Processing (NLP) and Machine Translation

- ▶ In **2013-2015**, **LSTMs** started achieving state-of-the-art results
 - ▶ Successful tasks include: handwriting recognition, speech recognition, machine translation, parsing, image captioning
 - ▶ LSTM became the dominant approach
- ▶ In **2019**, other approaches (e.g. **Transformers**) have become more dominant for certain tasks.
 - ▶ For example in **WMT** (a MT conference + competition):
 - ▶ In WMT 2016, the summary report contains "RNN" 44 times
 - ▶ In WMT 2018, the report contains "RNN" 9 times and "Transformer" 63 times
 - ▶ **Source:** "Findings of the 2016 Conference on Machine Translation (WMT16)", Bojar et al. 2016, <http://www.statmt.org/wmt16/pdf/W16-2301.pdf>
 - ▶ **Source:** "Findings of the 2018 Conference on Machine Translation (WMT18)", Bojar et al. 2018, <http://www.statmt.org/wmt18/pdf/WMT028.pdf>

Rapid Progress for NLP Pretraining (GLUE Benchmark)



More compute, more better?



Protein Folding Structure Prediction

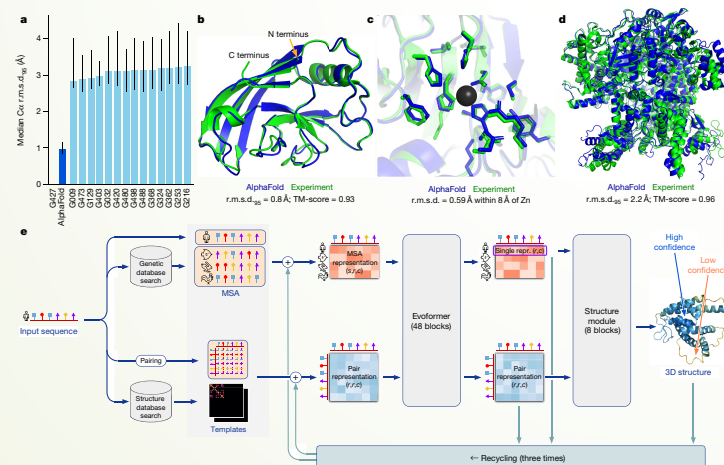
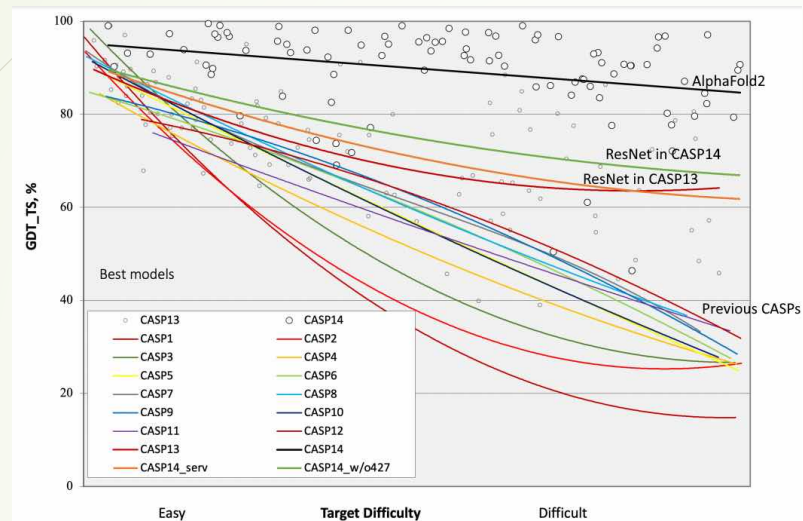


Fig. 1 | AlphaFold produces highly accurate structures. **a**, The performance of AlphaFold on the CASP14 dataset ($n = 87$ protein domains) relative to the top 15 entries (out of 146 entries), group numbers correspond to the numbers assigned to entrants by CASP. Data are median and the 95% confidence interval of the median, estimated from 10,000 bootstrap samples. **b**, Our prediction of CASP14 target T1049 (PDB 6Y4F, blue) compared with the true (experimental) structure (green). Four residues in the C-terminus of the crystal structure are B-factor outliers and are not depicted. **c**, CASP14 target T1056 (PDB 6Y1J).

An example of a well-predicted zinc-binding site (AlphaFold has accurately side chains even though it does not explicitly predict the zinc ion). **d**, CASP target T1044 (PDB 6VR4) – a 2,180-residue single chain – was predicted with correct domain packing (the prediction was made after CASP using AlphaFold without intervention). **e**, Model architecture. Arrows show the information flow among the various components described in this paper. Array shapes are shown in parentheses with s , number of sequences (N_{seq} in the main text); r , number of residues (N_{res} in the main text); c , number of channels.

Article

Highly accurate protein structure prediction with AlphaFold

<https://doi.org/10.1038/s41586-021-03819-2>

Received: 11 May 2021

Accepted: 12 July 2021

Published online: 15 July 2021

Open access

Check for updates

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Proteins are essential to life, and understanding their structure can facilitate a mechanistic understanding of their function. Through an enormous experimental effort^{1–4}, the structures of around 100,000 unique proteins have been determined⁵, but this represents a small fraction of the billions of known protein sequences^{6,7}. Structural coverage is bottlenecked by the months to years of painstaking effort required to determine a single protein structure. Accurate computational approaches are needed to address this gap and to enable large-scale structural bioinformatics. Predicting the three-dimensional structure that a protein will adopt based solely on its amino acid sequence – the structure prediction component of the ‘protein folding problem’⁸ – has been an important open research problem for more than 50 years⁹. Despite recent progress^{10–14}, existing methods fall far short of atomic accuracy, especially when no homologous structure is available. Here we provide the first computational method that can regularly predict protein structures with atomic accuracy even in cases in which no similar structure is known. We validated an entirely redesigned version of our neural network-based model, AlphaFold, in the challenging 14th Critical Assessment of protein Structure Prediction (CASP14)¹⁵, demonstrating accuracy competitive with experimental structures in a majority of cases and greatly outperforming other methods. Underpinning the latest version of AlphaFold is a novel machine learning approach that incorporates physical and biological knowledge about protein structure, leveraging multi-sequence alignments, into the design of the deep learning algorithm.

The development of computational methods to predict three-dimensional (3D) protein structures from the protein sequence has proceeded along two complementary paths that focus on either the physical interactions or the evolutionary history. The physical interaction programme heavily integrates our understanding of molecular driving forces into either thermodynamic or kinetic simulation of protein physics¹⁶ or statistical approximations thereof¹⁷. Although theoretically very appealing, this approach has proved highly challenging for even moderate-sized proteins due to the computational intractability of molecular simulation, the context dependence of protein stability and the difficulty of producing sufficiently accurate models of protein physics. The evolutionary programme has provided an alternative in recent years, in which the constraints on protein structure are derived from bioinformatics analysis of the evolutionary history of proteins, homology to solved structures^{18,19} and pairwise evolutionary correlations^{20–24}. This bioinformatics approach has benefited greatly from

the steady growth of experimental protein structures deposited in the Protein Data Bank (PDB)⁵, the explosion of genomic sequencing and the rapid development of deep learning techniques to interpret these correlations. Despite these advances, contemporary physical and evolutionary-history-based approaches produce predictions that are far short of experimental accuracy in the majority of cases in which a close homologue has not been solved experimentally and this has limited their utility for many biological applications.

In this study, we develop the first, to our knowledge, computational approach capable of predicting protein structures to near experimental accuracy in a majority of cases. The neural network AlphaFold that we developed was entered into the CASP14 assessment (May–July 2020; entered under the team name ‘AlphaFold2’ and a completely different model from our CASP13 AlphaFold system¹⁰). The CASP assessment is carried out biennially using recently solved structures that have not been deposited in the PDB or publicly disclosed so that it is a blind test

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AI for Science

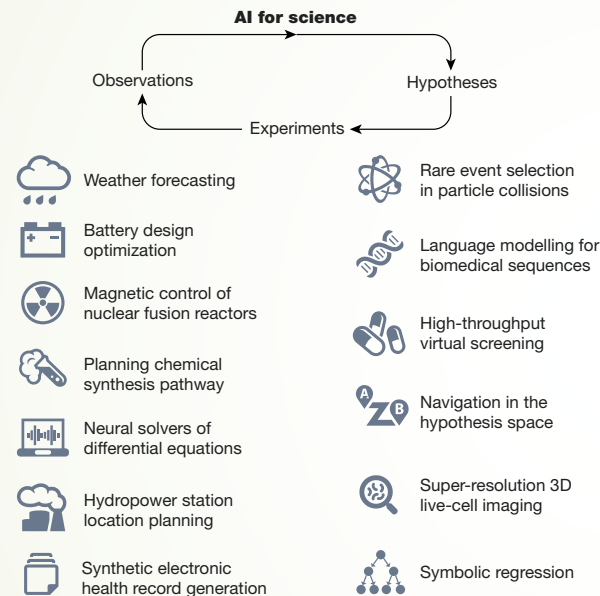


Fig. 1 | Science in the age of artificial intelligence. Scientific discovery is a multifaceted process that involves several interconnected stages, including hypothesis formation, experimental design, data collection and analysis. AI is poised to reshape scientific discovery by augmenting and accelerating research at each stage of this process. The principles and illustrative studies shown here highlight the contributions to enhance scientific understanding and discovery.

Review

Scientific discovery in the age of artificial intelligence

<https://doi.org/10.1038/s41586-023-06221-2>

Received: 30 March 2022

Accepted: 16 May 2023

Published online: 2 August 2023

Check for updates

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Artificial intelligence (AI) is being increasingly integrated into scientific discovery to augment and accelerate research, helping scientists to generate hypotheses, design experiments, collect and interpret large datasets, and gain insights that might not have been possible using traditional scientific methods alone. Here we examine breakthroughs over the past decade that include self-supervised learning, which allows models to be trained on vast amounts of unlabelled data, and geometric deep learning, which leverages knowledge about the structure of scientific data to enhance model accuracy and efficiency. Generative AI methods can create designs, such as small-molecule drugs and proteins, by analysing diverse data modalities, including images and sequences. We discuss how these methods can help scientists throughout the scientific process and the central issues that remain despite such advances. Both developers and users of AI tools need a better understanding of when such approaches need improvement, and challenges posed by poor data quality and stewardship remain. These issues cut across scientific disciplines and require developing foundational algorithmic approaches that can contribute to scientific understanding or acquire it autonomously, making them critical areas of focus for AI innovation.

The foundation for forming scientific insights and theories is laid by how data are collected, transformed and understood. The rise of deep learning in the early 2010s has significantly expanded the scope and ambition of these scientific discovery processes¹. Artificial intelligence (AI) is increasingly used across scientific disciplines to integrate massive datasets, refine measurements, guide experimentation, explore the space of theories compatible with the data, and provide actionable and reliable models integrated with scientific workflows for autonomous discovery.

Data collection and analysis are fundamental to scientific understanding and discovery, two of the central aims in science², and quantitative

methods and emerging technologies, from physical instruments such as microscopes to research techniques such as bootstrapping, have long been used to reach these aims³. The introduction of digitization in the 1950s paved the way for the general use of computing in scientific research. The rise of data science since the 2010s has enabled AI to provide valuable guidance by identifying scientifically relevant patterns from large datasets.

Although scientific practices and procedures vary across stages of scientific research, the development of AI algorithms cuts across traditionally isolated disciplines (Fig. 1). Such algorithms can enhance the design and execution of scientific studies. They are becoming

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ChatGPT (GPT 3.5-4)

ChatGPT

🌐 94 languages ▾

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From Wikipedia, the free encyclopedia



ChatGPT, which stands for **Chat Generative Pre-trained Transformer**, is a [large language model](#)-based [chatbot](#) developed by [OpenAI](#) and launched on November 30, 2022, notable for enabling users to refine and steer a conversation towards a desired length, format, style, level of detail, and [language](#) used. Successive prompts and replies, known as [prompt engineering](#), are considered at each conversation stage as a context.^[2]

ChatGPT is built upon [GPT-3.5](#) and [GPT-4](#) —members of OpenAI's proprietary series of [generative pre-trained transformer](#) (GPT) models, based on the [transformer](#) architecture developed by [Google](#)^[3]—and it is [fine-tuned](#) for conversational applications using a combination of [supervised](#) and [reinforcement learning](#) techniques.^[4] ChatGPT was released as a freely available research preview, but due to its popularity, OpenAI now operates the service on a [freemium model](#). It allows users on its free tier to access the GPT-3.5-based version. In contrast, the more advanced GPT-4 based version and priority access to newer features are provided to paid subscribers under the commercial name "ChatGPT Plus".

By January 2023, it had become what was then the fastest-growing consumer software application in history, gaining over 100 million users and contributing to OpenAI's [valuation](#) growing to [US\\$29 billion](#).^{[5][6]} Within months, [Google](#), [Baidu](#), and [Meta](#) accelerated the development of their competing products: [Bard](#), [Ernie Bot](#), and [LLaMA](#).^[7] Microsoft launched its [Bing Chat](#) based on OpenAI's GPT-4. Some observers expressed concern over the potential of ChatGPT to displace or atrophy [human intelligence](#) and its potential to enable [plagiarism](#) or fuel [misinformation](#).^{[4][8]}

Training

ChatGPT is based on particular [GPT foundation models](#), namely [GPT-3.5](#) and [GPT-4](#), that were [fine-tuned](#) to target conversational usage.^[9] The fine-tuning process leveraged both [supervised learning](#) as well as

ChatGPT



Developer(s)	OpenAI
Initial release	November 30, 2022; 9 months ago
Stable release	August 3, 2023; 31 days ago ^[1]
Written in	Python
Engine	GPT-3.5 GPT-4
Platform	Cloud computing platforms
Type	Chatbot Large language model Generative text-to-image model Generative pre-trained transformer
License	Proprietary
Website	chat.openai.com/chat

AI for Math?



For favour of Posting

THE HONG KONG UNIVERSITY OF SCIENCE & TECHNOLOGY

Department of Mathematics

SEMINAR ON DATA SCIENCE AND APPLIED MATHEMATICS

Solving olympiad geometry without human demonstrations

By

Dr. Trieu H. TRINH
New York University

Abstract

Proving mathematical theorems at the olympiad level represents a notable milestone in human-level automated reasoning, owing to their reputed difficulty among the world's best talents in pre-university mathematics. Current machine-learning approaches, however, are not applicable to most mathematical domains owing to the high cost of translating human proofs into machine-verifiable format. The problem is even worse for geometry because of its unique translation challenges, resulting in severe scarcity of training data. We propose AlphaGeometry, a theorem prover for Euclidean plane geometry that sidesteps the need for human demonstrations by synthesizing millions of theorems and proofs across different levels of complexity. AlphaGeometry is a neuro-symbolic system that uses a neural language model, trained from scratch on our large-scale synthetic data, to guide a symbolic deduction engine through infinite branching points in challenging problems. On a test set of 30 latest olympiad-level problems, AlphaGeometry solves 25, outperforming the previous best method that only solves ten problems and approaching the performance of an average International Mathematical Olympiad (IMO) gold medalist. Notably, AlphaGeometry produces human-readable proofs, solves all geometry problems in the IMO 2000 and 2015 under human expert evaluation and discovers a generalized version of a translated IMO theorem in 2004.

Biography

Trieu recently graduated from his PhD program at New York University in January 2024. Prior to NYU, he worked for 2 years at Google Brain. His research covers a wide range of topics: Self-supervised learning in images, long term dependencies in RNNs, Commonsense reasoning in LLMs, and most recently mathematical reasoning.

Date : 6 February 2024 (Tuesday)

Time : 2:00pm

Zoom Meeting : <https://hkust.zoom.us/j/5616960008>
(Passcode: hkust)

All are Welcome!

Article

Solving olympiad geometry without human demonstrations

<https://doi.org/10.1038/s41586-023-06747-5>

Trieu H. Trinh^{1,2*}, Yuhuai Wu¹, Quoc V. Le¹, He He² & Thang Luong^{1,2*}

Received: 30 April 2023

Accepted: 13 October 2023

Published online: 17 January 2024

Open access

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Proving mathematical theorems at the olympiad level represents a notable milestone in human-level automated reasoning^{1–4}, owing to their reputed difficulty among the world's best talents in pre-university mathematics. Current machine-learning approaches, however, are not applicable to most mathematical domains owing to the high cost of translating human proofs into machine-verifiable format. The problem is even worse for geometry because of its unique translation challenges^{1,5}, resulting in severe scarcity of training data. We propose AlphaGeometry, a theorem prover for Euclidean plane geometry that sidesteps the need for human demonstrations by synthesizing millions of theorems and proofs across different levels of complexity. AlphaGeometry is a neuro-symbolic system that uses a neural language model, trained from scratch on our large-scale synthetic data, to guide a symbolic deduction engine through infinite branching points in challenging problems. On a test set of 30 latest olympiad-level problems, AlphaGeometry solves 25, outperforming the previous best method that only solves ten problems and approaching the performance of an average International Mathematical Olympiad (IMO) gold medalist. Notably, AlphaGeometry produces human-readable proofs, solves all geometry problems in the IMO 2000 and 2015 under human expert evaluation and discovers a generalized version of a translated IMO theorem in 2004.

Proving theorems showcases the mastery of logical reasoning and the ability to search through an infinitely large space of actions towards a target, signifying a remarkable problem-solving skill. Since the 1950s (refs. 6,7), the pursuit of better theorem-proving capabilities has been a constant focus of artificial intelligence (AI) research⁸. Mathematical olympiads are the most reputed theorem-proving competitions in the world, with a similarly long history dating back to 1959, playing an instrumental role in identifying exceptional talents in problem solving. Matching top human performances at the olympiad level has become a notable milestone of AI research^{2–4}.

Theorem proving is difficult for learning-based methods because training data of human proofs translated into machine-verifiable languages are scarce in most mathematical domains. Geometry stands out among other olympiad domains because it has very few proof examples in general-purpose mathematical languages such as Lean⁹ owing to translation difficulties unique to geometry^{1,5}. Geometry-specific languages, on the other hand, are narrowly defined and thus unable to express many human proofs that use tools beyond the scope of geometry, such as complex numbers (Extended Data Figs. 3 and 4). Overall, this creates a data bottleneck, causing geometry to lag behind in recent progress that uses human demonstrations^{2–4}. Current approaches to geometry, therefore, still primarily rely on symbolic methods and human-designed, hard-coded search heuristics^{10–14}.

We present an alternative method for theorem proving using synthetic data, thus sidestepping the need for translating human-provided proof examples. We focus on Euclidean plane geometry and exclude topics such as geometric inequalities and combinatorial geometry.

By using existing symbolic engines on a diverse set of random theorem premises, we extracted 100 million synthetic theorems and their proofs, many with more than 200 proof steps, four times longer than the average proof length of olympiad theorems. We further define and use the concept of dependency difference in synthetic proof generation, allowing our method to produce nearly 10 million synthetic proof steps that construct auxiliary points, reaching beyond the scope of pure symbolic deduction. Auxiliary construction is geometry's instance of exogenous term generation, representing the infinite branching factor of theorem proving, and widely recognized in other mathematical domains as the key challenge to proving many hard theorems^{1,2}. Our work therefore demonstrates a successful case of generating synthetic data and learning to solve this key challenge. With this solution, we present a general guiding framework and discuss its applicability to other domains in Methods section 'AlphaGeometry framework and applicability to other domains'.

We pretrain a language model on all generated synthetic data and fine-tune it to focus on auxiliary construction during proof search, delegating all deduction proof steps to specialized symbolic engines. This follows standard settings in the literature, in which language models such as GPT-f (ref. 15), after being trained on human proof examples, can generate exogenous proof terms as inputs to fast and accurate symbolic engines such as nlinerith or ring^{13,16}, using the best of both worlds. Our geometry theorem prover AlphaGeometry, illustrated in Fig. 1, produces human-readable proofs, substantially outperforms the previous state-of-the-art geometry-theorem-proving computer program and approaches the performance of an average IMO gold

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Number of AI papers on arXiv, 2010-2019

Number of AI papers on arXiv, 2010-2019

Source: arXiv, 2019.

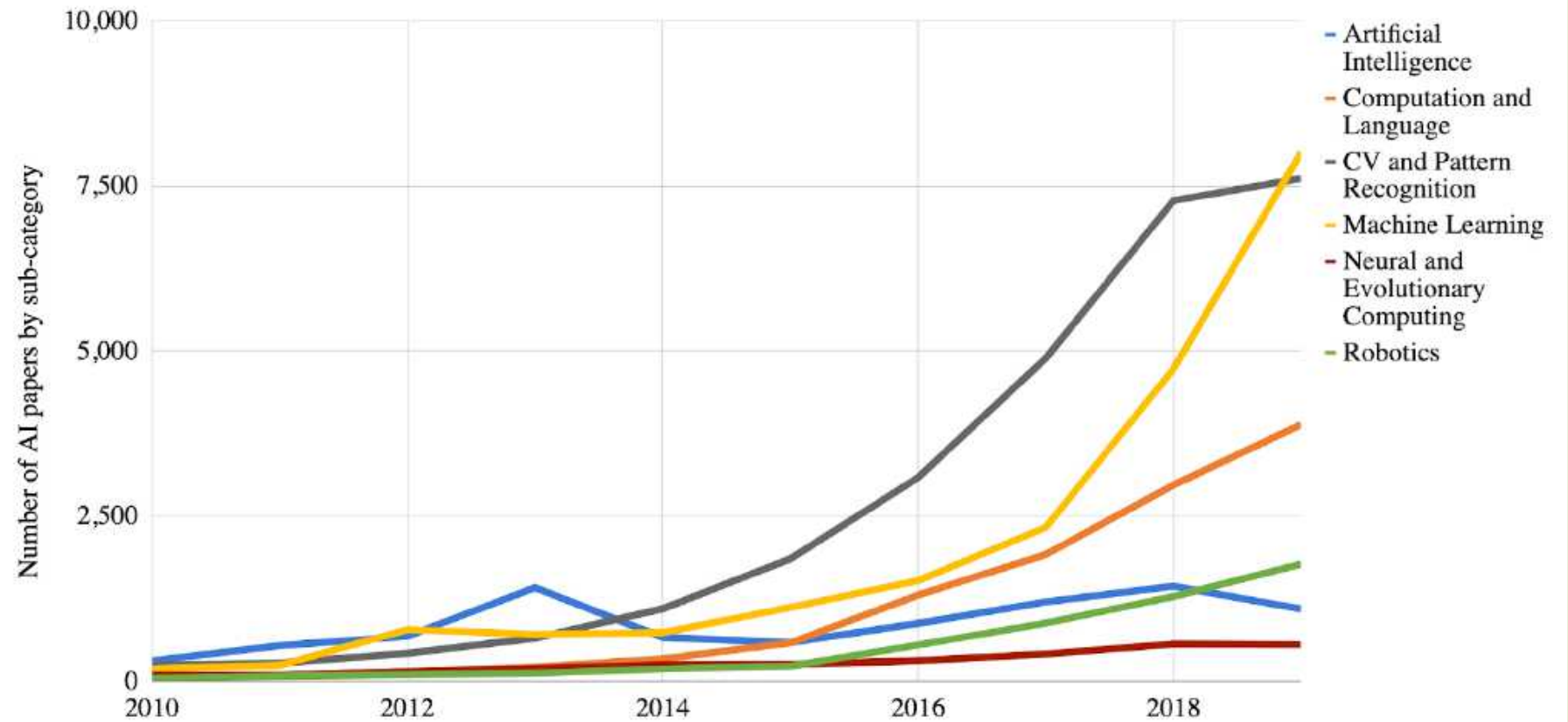
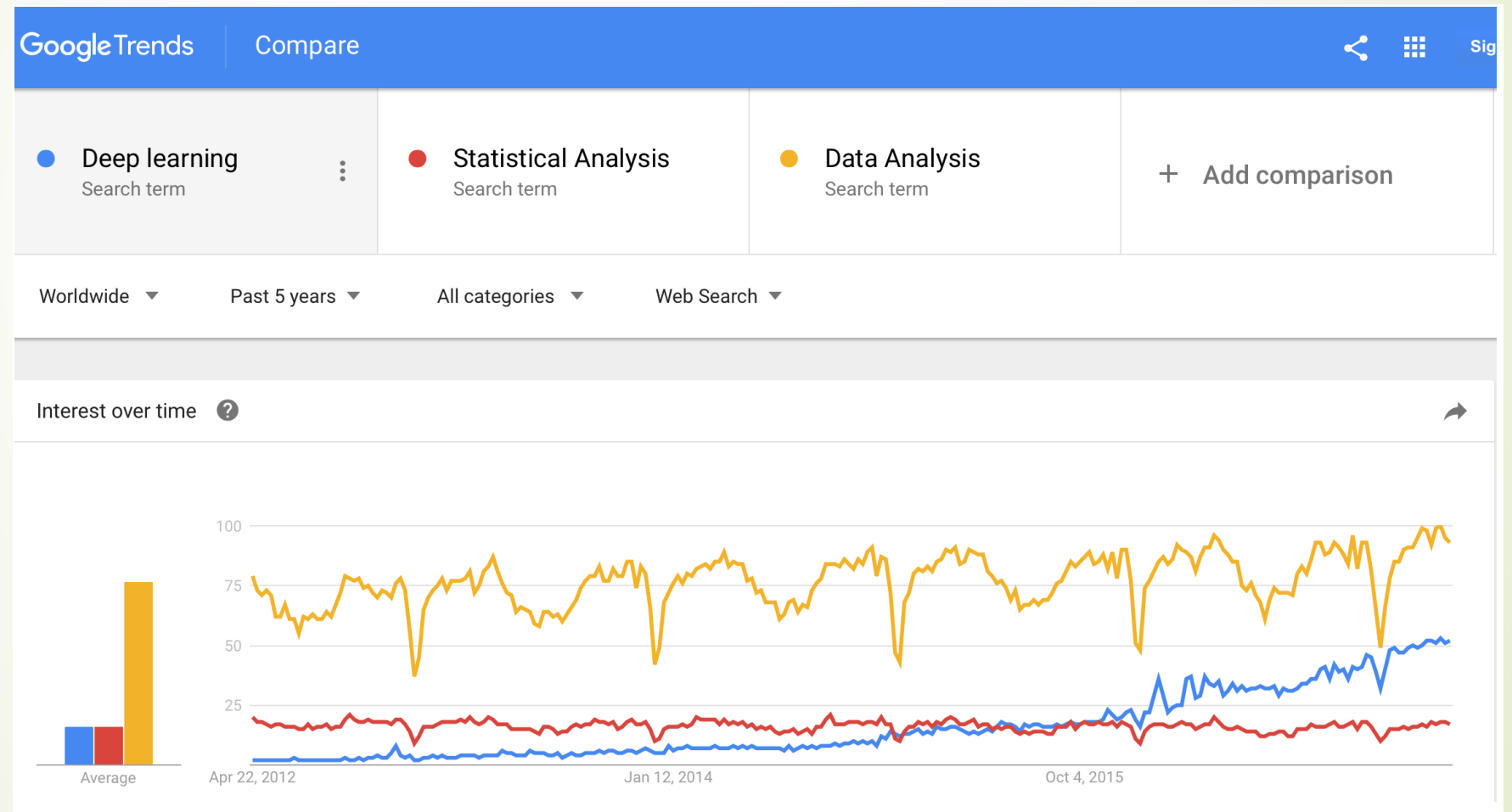


Fig. 1.6.

Growth of Deep Learning

'Deep Learning' is coined by Hinton et al. in their Restricted Boltzman Machine paper, *Science* 2006, not yet popular until championing ImageNet competitions.



Some Cold Water: Tesla Autopilot Misclassifies Truck as Billboard



Problem: Why? How can you trust a blackbox?

Deep Learning may be fragile in generalization against noise!


 x

“panda”

57.7% confidence

 $+ .007 \times$

 $\text{sign}(\nabla_x J(\theta, x, y))$

“nematode”

8.2% confidence

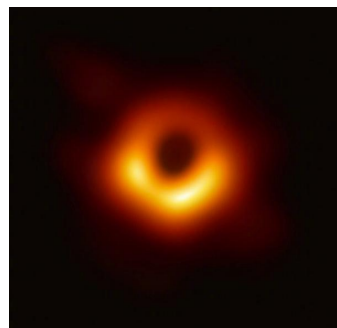
 $=$

 $x +$
 $\epsilon \text{sign}(\nabla_x J(\theta, x, y))$

“gibbon”

99.3 % confidence

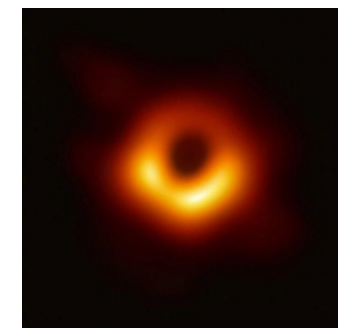
[Goodfellow et al., 2014]



“black hole”

87.7% confidence

 $+ .007 \times$

 $=$


“donut”

99.3% confidence



CNN learns **texture** features, not **shapes**



(a) Texture image
81.4% **Indian elephant**
10.3% indri
8.2% black swan



(b) Content image
71.1% **tabby cat**
17.3% grey fox
3.3% Siamese cat



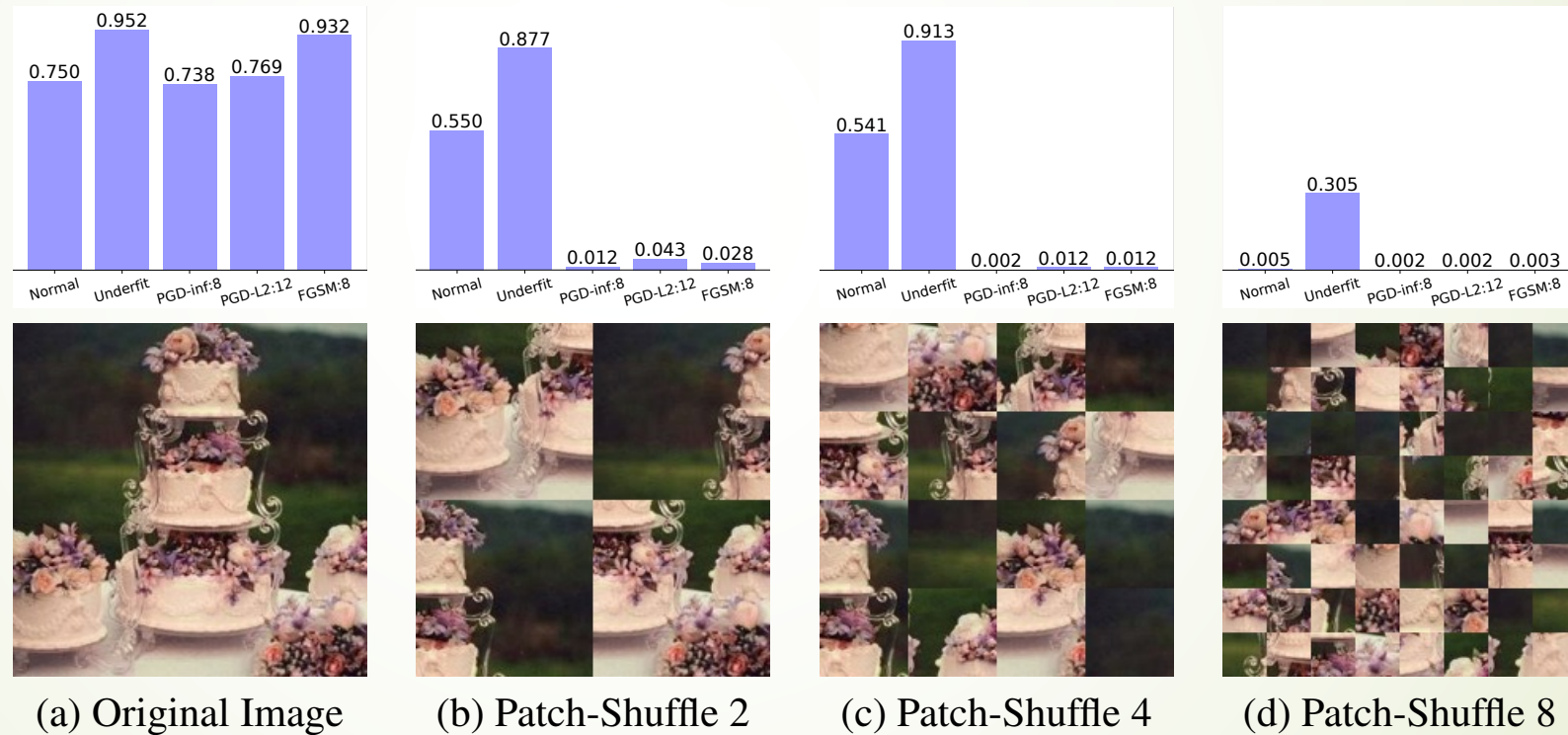
(c) Texture-shape cue conflict
63.9% **Indian elephant**
26.4% indri
9.6% black swan

Geirhos et al. ICLR 2019

<https://videoken.com/embed/W2HvLBMhCJQ?tocitem=46>

Lack of Causality or Interpretability

- ImageNet training learns non-semantic texture features: after random shuffling of patches, shapes information are destroyed which does not affect CNN's performance much.

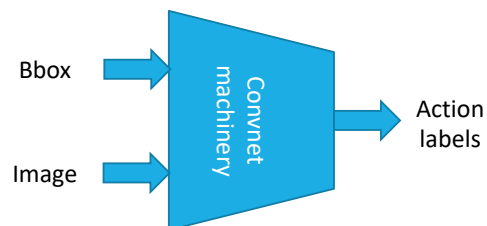
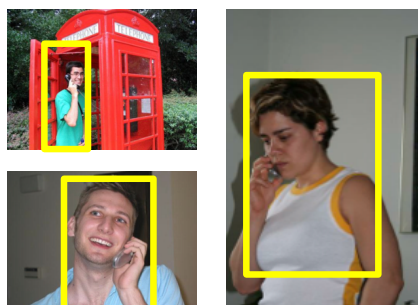


Capture spurious correlations and can't do causal inference on **counterfactuals**

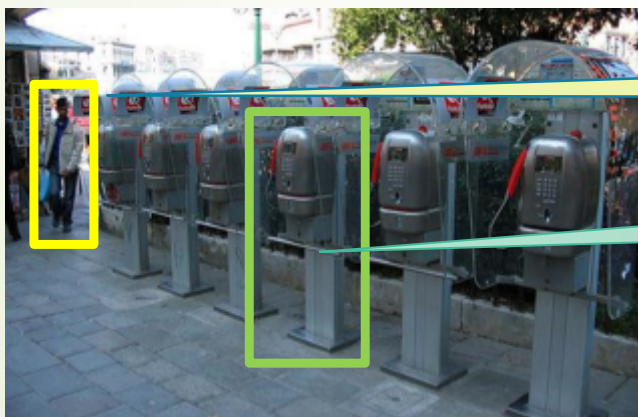
<https://videoken.com/embed/8UxS4ls6g1g?tocitem=2>

Leon Bottou, ICLR 2019

Example: detection of the action "giving a phone call"



(Oquab et al., CVPR 2014)
~70% correct (SOTA in 2014)



Not giving a phone call.

Giving a phone call ????

Overfitting causes **privacy leakage**

- ▶ Model inversion attack leaks privacy



Figure: Recovered (Left), Original (Right)

What's wrong with deep learning?

Ali Rahimi NIPS'17: Machine (deep) Learning has become **alchemy**.


<https://www.youtube.com/watch?v=ORHFOndEzPc>

Yann LeCun CVPR'15, invited talk: **What's wrong with deep learning?**
One important piece: **missing some theory (clarity in understanding)!**

<http://techtalks.tv/talks/whats-wrong-with-deep-learning/61639/>



Being alchemy is certainly not a shame, not wanting to work on advancing to chemistry is a shame! -- **by Eric Xing**



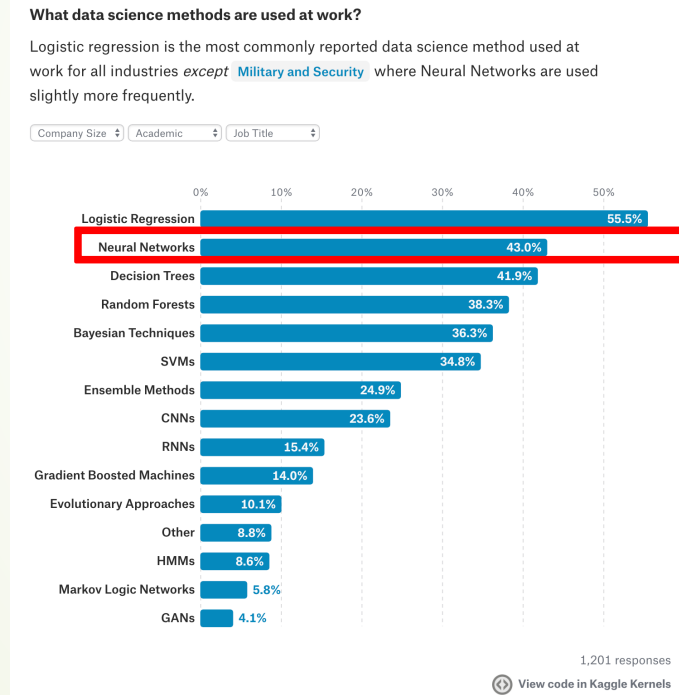
“ Shall we see soon an
emergence
from Alchemy to Science
in deep leaning? ”

How can we teach our students in the next generation science rather than alchemy?

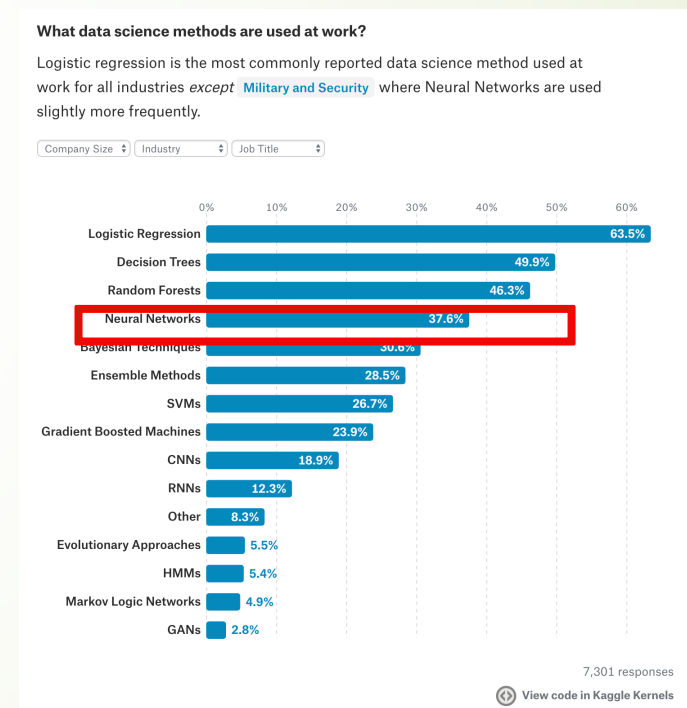
Kaggle survey: Top Data Science Methods

<https://www.kaggle.com/surveys/2017>

Academic



Industry



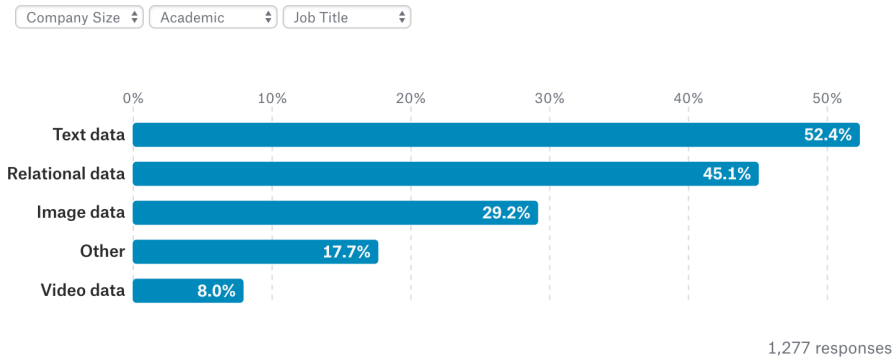
What type of data is used at work?

<https://www.kaggle.com/surveys/2017>

Academic

What type of data is used at work?

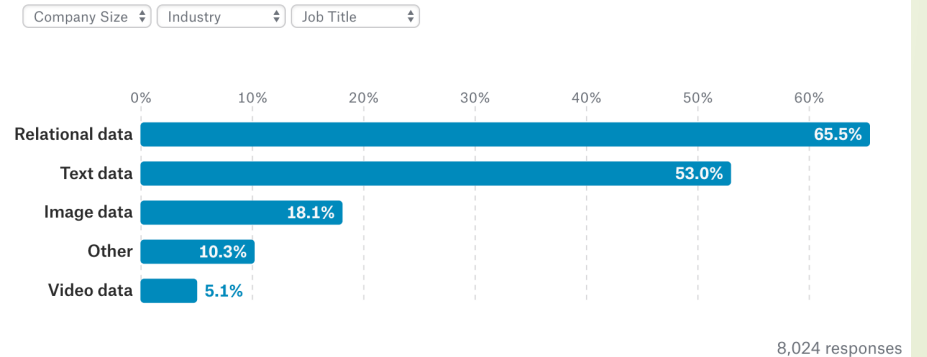
Relational data is the most commonly reported type of data used at work for all industries except for **Academia** and the **Military and Security** industry where text data's used more.



Industry

What type of data is used at work?

Relational data is the most commonly reported type of data used at work for all industries except for **Academia** and the **Military and Security** industry where text data's used more.



All models are wrong, but some are useful ...

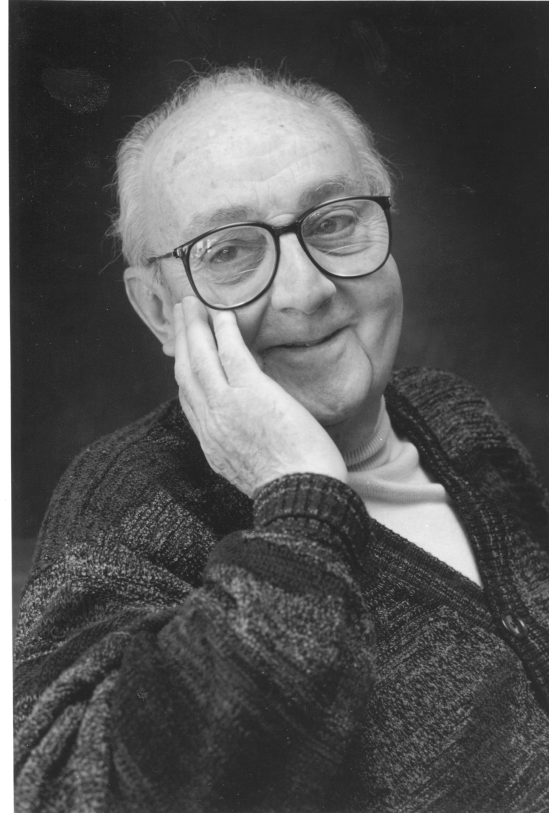
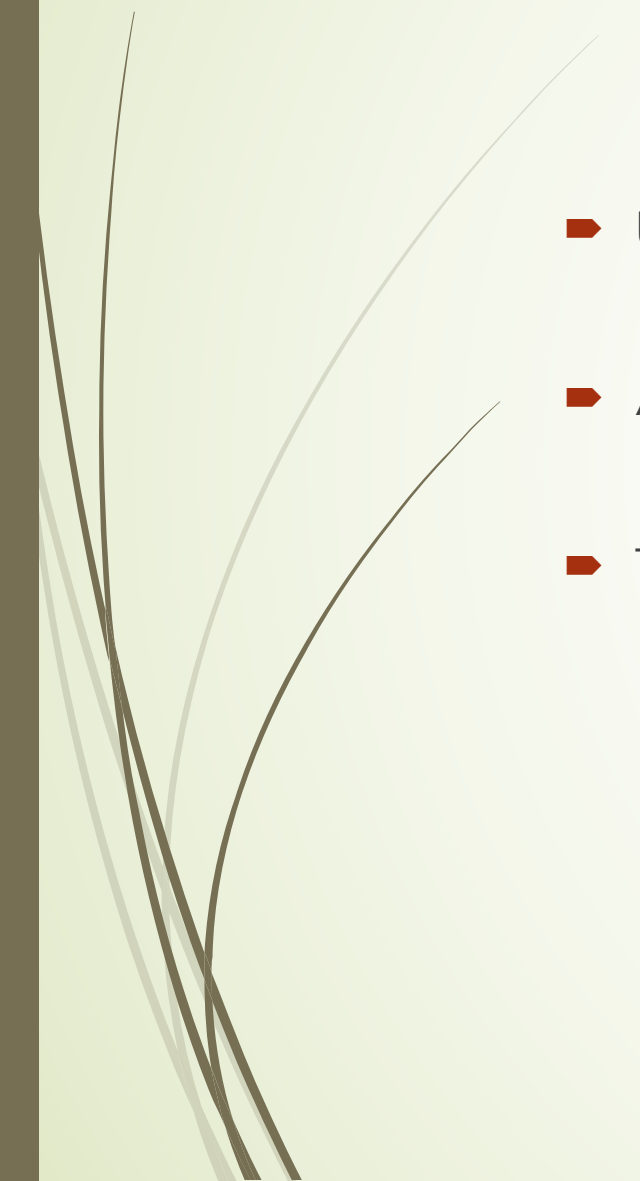


Figure 7: George Box: "Essentially, all models are wrong, but some are useful."



In this class

- Understand its principles: statistics, optimization
 - Analyze the real world data with the methods
 - Team-work in projects
- 

Thank you!

